## GCSE Mathematics 1MA0

Formulae: Higher Tier
You must not write on this formulae page.
Anything you write on this formulae page will gain NO credit.

Volume of prism $=$ area of cross section $\times$ length


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


In any triangle $A B C$


Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$

Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


The Quadratic Equation
The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$, are given by
$x=\frac{-b \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

## Answer ALL questions.

## Write your answers in the spaces provided.

You must write down all stages in your working.
1 (a) Use your calculator to work out $\frac{\sqrt{7056}}{0.35 \times 12.8}$
Write down all the figures on your calculator display.
You must give your answer as a decimal.
(b) Write your answer to part (a) correct to 1 significant figure.
(1)

2 Pavel and Katie share some sweets in the ratio 3:8
Katie gets 32 sweets.
(a) How many sweets does Pavel get?

Katie also has a tin of chocolates.
There are 80 chocolates in the tin.
$45 \%$ of the chocolates have toffee in the middle.
(b) Work out the number of chocolates that have toffee in the middle.

$$
\begin{aligned}
50 \% & =40 \\
5 \% & =4 \\
45 \% & =36
\end{aligned}
$$

3 Bill has some counters in a bag.

$$
\left.\begin{array}{l}
3 \text { of the counters are red. } \\
7 \text { of the counters are blue. }
\end{array}\right\} 10
$$

The rest of the counters are yellow.
Bill takes at random a counter from the bag.
The probability that he takes a yellow counter is $\frac{2}{7}$
How many yellow counters are in the bag before Bill takes a counter?

$$
\begin{aligned}
& \frac{5}{7} \text { is } 10 \\
& \frac{1}{7} \text { is } 2 \\
& \frac{2}{7} \text { is } 4
\end{aligned}
$$

4 The diagram shows a solid prism.


On the centimetre square grid, draw the side elevation of the solid prism from the direction shown by the arrow.

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

5 Ben goes on holiday to Hong Kong.
In Hong Kong, Ben sees a camera costing HK\$3179.55
In London, an identical camera costs $£ 285$
The exchange rate is $£ 1=\mathrm{HK} \$ 12.30$
Ben buys the camera in Hong Kong.
How much cheaper is the camera in Hong Kong than in London?

$$
\begin{aligned}
& \text { In Hong Kong: } \\
& \quad 3179.55 \div 12.30=z 258.50
\end{aligned}
$$

$$
285-258.5= \pm 26.50
$$

6 There are 130 adults at a language school.
Each adult studies one of French or Spanish or German.

> 96 of the adults are women.
> 12 of the women study French.
> 73 of the adults study Spanish.
> 55 of the women study Spanish.
> 9 of the men study German.

How many of the adults study French?

*7 Plants are sold in three different sizes of tray.
A small tray of 30 plants costs $£ 6.50$
A medium tray of 40 plants costs $£ 8.95$
A large tray of 50 plants costs $£ 10.99$
Gaz wants to buy the tray of plants that is the best value for money.
Which size tray of plants should she buy?
You must show all your working.

$$
\begin{aligned}
& \text { Cost per plant: } \\
& \text { small tray } \frac{\text { t6.50 }}{30}=0.216 \\
& \text { medium tray } \frac{t 8.95}{40}=0.22375 \\
& \text { Large tray } \frac{\text { E10.99 }}{50}=0.2198 \\
& \text { The small tray is better value. }
\end{aligned}
$$

8 Here are the first four terms of an arithmetic sequence.
3
10
17
24
(a) Find, in terms of $n$, an expression for the $n$th term of this arithmetic sequence.
(b) Is 150 a term of this sequence?

You must explain how you get your answer.
150 is a term of the sequence.
If you add 4, then divide by seven you get a whole number. 150 is
$22^{\text {nd }}$ term in the sequence.
(Total for Question 8 is 4 marks)

9 The diagram shows a pattern using four identical rhombuses.


Diagram NOT accurately drawn

Work out the size of the angle marked $a$. You must show your working.

$$
\begin{array}{cl}
360-100 & =260 \\
\frac{260}{4}=65^{\circ} & \begin{array}{l}
\text { Angler in } \\
\text { circle }=360^{\circ}
\end{array} \\
360-(2 \times 65)=230 & \begin{array}{l}
\text { Angles in } \\
\text { quadrilateral } \\
\text { equal } 360^{\circ}
\end{array}
\end{array}
$$

10 Sasha takes a music exam.
The table shows the result that Sasha can get for different percentages in her music exam.

| Percentage | Result |
| :---: | :---: |
| $50 \%-69 \%$ | Pass |
| $70 \%-84 \%$ | Merit |
| $85 \%-100 \%$ | Distinction |

Sasha gets 62 out of 80 in her music exam.
What result does Sasha get?
You must show your working.

$$
\frac{62}{80} \times 100=77.5 \%
$$

(Total for Question 10 is $\mathbf{3}$ marks)

11 (a) Simplify $x^{7} \times x^{3}$
(10
(1)
(b) Simplify $\left(m^{4}\right)^{3}$

(1)
(c) Simplify $\frac{36 a f^{8}}{12 a^{5} f^{2}}$
(2)

12 A circle has a diameter of 140 cm .
Work out the circumference of the circle.
Give your answer correct to 3 significant figures.

$$
\begin{aligned}
& 2 \times \pi \times r \\
= & 2 \times \pi \times 70 \\
= & 439.8229715
\end{aligned}
$$

$$
440
$$

(Total for Question 12 is 2 marks)

14 The table gives information about the temperature, $T^{\circ} \mathrm{C}$, at noon in a town for 50 days.

| Temperature ( $T^{\circ} \mathrm{C}$ ) |  | Frequency | 60 |
| :---: | :---: | :---: | :---: |
| $8<T \leqslant 12$ | $10 \times$ | 6 |  |
| $12<T \leqslant 16$ | $14 \times$ | 8 | 112 |
| $16<T \leqslant 20$ | $18 \times$ | 13 | 234 |
| $20<T \leqslant 24$ | $22 x$ | 21 | $462$ |
| $24<T \leqslant 28$ | $26 x$ | 2 | $52$ |
| al class interval. |  |  | 920 |

(a) Write down the modal class interval.

$$
20<T \leqslant 24
$$

(1)
(b) Calculate an estimate for the mean temperature.

$$
920 \div 50
$$

(c) Draw a frequency polygon for the information in the table.

(2)
(Total for Question 14 is 7 marks)

15 Here is a right-angled triangle.


Diagram NOT
accurately drawn

Work out the length of $A C$.
Give your answer correct to 1 decimal place.

$$
\begin{aligned}
39^{2}+70^{2} & =x^{2} \\
6421 & =x^{2} \\
\sqrt{6421} & =x \\
x & =80.1 \quad(1 \mathrm{dp})
\end{aligned}
$$

80.1 cm

17 (a) Complete the table of values for $y=x^{3}-4 x$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -15 | 0 | 3 | 0 | -3 | 0 | 15 |

(b) On the grid, draw the graph of $y=x^{3}-4 x$ from $x=-3$ to $x=3$

(2)
(Total for Question 17 is 4 marks)
$18 A B C$ is an isosceles triangle.


Work out the area of the triangle.
Give your answer correct to 3 significant figures.
(0) (4)

$$
\begin{aligned}
\tan (54) & =\frac{x}{6} \\
x & =6 \tan (54) \\
x & =8.258 \ldots
\end{aligned}
$$

Area $=\frac{1}{2} \times 12 \times$ ANS

$$
=49.5 \mathrm{~cm}^{2} \quad(3 s t)
$$

$$
49.5 \mathrm{~cm}^{2}
$$

19 (a) Write $7.8 \times 10^{-4}$ as an ordinary number.

$$
0.00078
$$

(1)
(b) Write 95600000 as a number in standard form.

$$
9.56 \times 10^{7}
$$

20 In a sale normal prices are reduced by $20 \%$.
A washing machine has a sale price of $£ 464$
By how much money is the normal price of the washing machine reduced?

$$
\begin{aligned}
& t 464=80 \% \\
& t 580=1 \% \\
& t 580=100 \%
\end{aligned}
$$

$$
£ 580-£ 464=£ 116
$$

$$
\text { £ } 116
$$

22 The diagram shows a trapezium.


Diagram NOT accurately drawn

All the measurements are in centimetres.
The area of the trapezium is $351 \mathrm{~cm}^{2}$.
(a) Show that $2 x^{2}+x-351=0$

$$
\begin{align*}
\text { Area } & =\frac{x+5+x-4}{2} \times 20 \\
351 & =\left(\frac{2 x+1}{2}\right) 2 x  \tag{2}\\
351 & =\frac{4 x^{2}+2 x}{2}
\end{align*}
$$

(b) Work out the value of $x$.

$$
0=2 x^{2}+x-351
$$

$$
\begin{aligned}
& (2 x+27)(x-13)=0 \\
& x=-\frac{27}{2} \quad x=13
\end{aligned}
$$

$$
x \text { cannot te negative }
$$

$$
\therefore x=13 \mathrm{~cm}
$$

(3)
(Total for Question 22 is 5 marks)

