## Edexcel GCE

## Core Mathematics C2

Advanced Subsidiary

# Binomial Expansion 

Materials required for examination
Mathematical Formulae (Pink or Green)

Items included with question papers Nil

## Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
You must show sufficient working to make your methods clear to the Examiner.
Answers without working may not gain full credit.

1. Find the first three terms, in ascending powers of $x$, of the binomial expansion of $(3+2 x)^{5}$, giving each term in its simplest form.
2. Find the first 3 terms, in ascending powers of $x$, of the binomial expansion of $(3-2 x)^{5}$, giving each term in its simplest form.
3. (a) Find the first 3 terms, in ascending powers of $x$, of the binomial expansion of

$$
(2+k x)^{7}
$$

where $k$ is a constant. Give each term in its simplest form.

Given that the coefficient of $x^{2}$ is 6 times the coefficient of $x$,
(b) find the value of $k$.
4. (a) Find the first 4 terms, in ascending powers of $x$, of the binomial expansion of $(1+a x)^{10}$, where $a$ is a non-zero constant. Give each term in its simplest form.

Given that, in this expansion, the coefficient of $x^{3}$ is double the coefficient of $x^{2}$,
(b) find the value of $a$.
5. (a) Find the first 4 terms of the expansion of $\left(1+\frac{x}{2}\right)^{10}$ in ascending powers of $x$, giving each term in its simplest form.
(b) Use your expansion to estimate the value of $(1.005)^{10}$, giving your answer to 5 decimal places.
(3)
6. (a) Find the first four terms, in ascending powers of $x$, in the bionomial expansion of $(1+k x)^{6}$, where $k$ is a non-zero constant.

Given that, in this expansion, the coefficients of $x$ and $x^{2}$ are equal, find
(b) the value of $k$,
(c) the coefficient of $x^{3}$.
7. (a) Find the first 4 terms, in ascending powers of $x$, of the binomial expansion of $(1-2 x)^{5}$. Give each term in its simplest form.
(b) If $x$ is small, so that $x^{2}$ and higher powers can be ignored, show that

$$
\begin{equation*}
(1+x)(1-2 x)^{5} \approx 1-9 x . \tag{2}
\end{equation*}
$$

8. Find the first 3 terms, in ascending powers of $x$, of the binomial expansion of $(2+x)^{6}$, giving each term in its simplest form.
9. (a) Find the first 3 terms, in ascending powers of $x$, of the binomial expansion of

$$
(1+p x)^{9}
$$

where $p$ is a constant.

The first 3 terms are $1,36 x$ and $q x^{2}$, where $q$ is a constant.
(b) Find the value of $p$ and the value of $q$.
10. (a) Write down the first three terms, in ascending powers of $x$, of the binomial expansion of $(1+p x)^{12}$, where $p$ is a non-zero constant.

Given that, in the expansion of $(1+p x)^{12}$, the coefficient of $x$ is $(-q)$ and the coefficient of $x^{2}$ is $11 q$,
(b) find the value of $p$ and the value of $q$.

