

Write your name here

Surname

Other Names

# AS/A Level Mathematics

## Integration

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled..
- Answer the questions in the spaces provided  
– there may be more space than you need.
- You should show sufficient working to make your methods clear.  
Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

### Information

- The marks for **each** question are shown in brackets  
– use this as a guide as to how much time to spend on each question.

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

1  $y = 2x^3 + 5x^2 - 7x + 10$

Find  $\int y \, dx$

(Total for question 1 is 4 marks)

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2 Find  $\int (3x^2 + 7x - 2) \, dx$

(Total for question 2 is 4 marks)

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3 Find  $\int (x + 4)(x - 3) \, dx$

(Total for question 3 is 4 marks)

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4  $f'(x) = 6x^2 - 3x + 8$

Given that the point (1, 8) lies on  $y = f(x)$

Find an expression for  $f(x)$

(Total for question 4 is 5 marks)

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5  $y = 4\sqrt{x} + \frac{1}{x^2} + 10$

Find  $\int y \, dx$

(Total for question 5 is 4 marks)

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6 Find  $\int_1^3 (x + 4)(x - 3) \, dx$

(Total for question 6 is 5 marks)

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7  $\frac{dy}{dx} = 10x^4 - 5$

Given that the point (2, 30) lies on the curve

Find an expression for  $y$  in terms of  $x$

(Total for question 7 is 5 marks)

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8 Find  $\int_1^4 5 + \frac{1}{\sqrt{x}} \, dx$

(Total for question 8 is 5 marks)

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9 The curve with the equation  $f(x)$  passes through the point (1, 2)

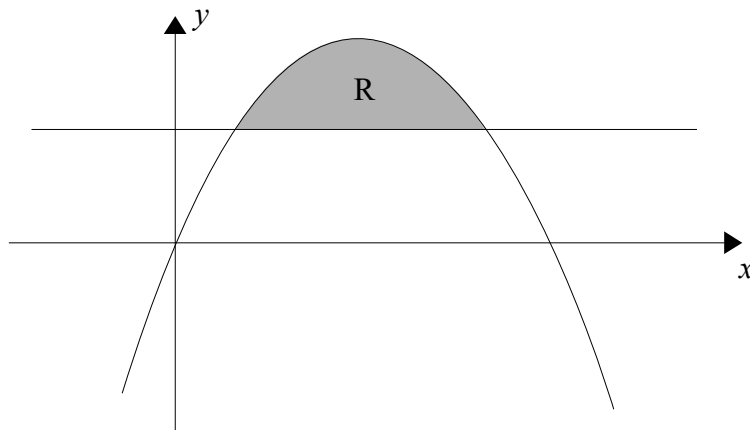
Given that  $f'(x) = 5 + \frac{3x^2 + 2}{x^{\frac{1}{2}}}$

Find  $f(x)$  giving your answer in its simplest form.

(Total for question 9 is 7 marks)

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10

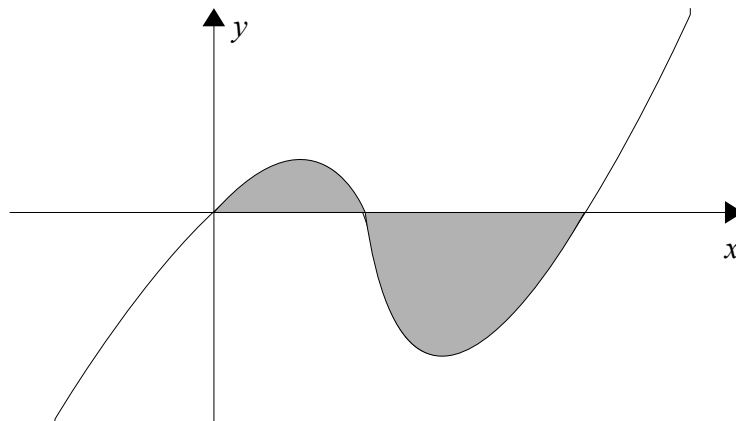


The sketch shows the curve  $y = x(5 - x)$  and the line  $y = 4$

- (a) Find the coordinates of the points where the line intersects the curve. (2)
- (b) Find the area of the shaded region R. (6)

(Total for question 10 is 8 marks)

11

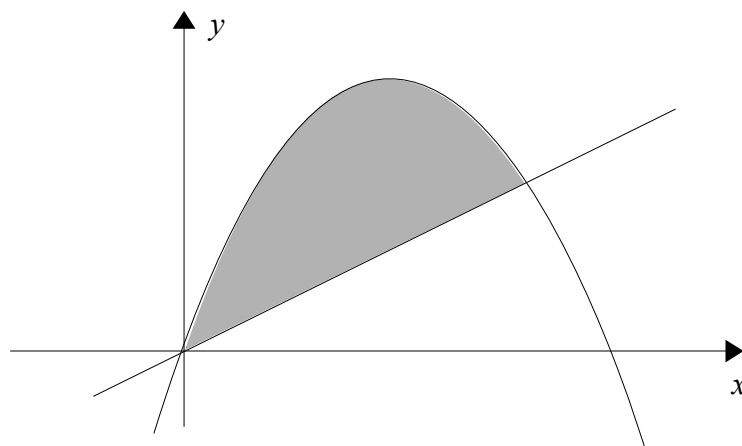


The sketch shows the curve  $y = x(x - 2)(x - 5)$

- (a) Write down the values of  $x$  where the curve crosses the  $x$  axis. (1)
- (b) Find the area of the shaded region. (8)

(Total for question 11 is 9 marks)

12



The sketch shows the curve  $y = 10x - x^2$  and the straight line  $y = 2x$

- (a) Find the coordinates of the points where the line intersects the curve. (2)
- (b) Find the area of the shaded region. (6)

(Total for question 12 is 8 marks)