

- a) · The probability is close to 0.5
· A large number of trials.

$$\begin{aligned} b) \quad \mu &= np = 30(0.4) & \sigma^2 &= np(1-p) \\ &= \underline{\underline{12}} & &= 30(0.4)(0.6) \\ & & &= 7.2 \\ & & \sigma &= \underline{\underline{\sqrt{7.2}}} \end{aligned}$$

8: upper bound 8.5
lower bound 7.5

$$P(X < 7.5) = \underline{\underline{0.0468}} \text{ (3sf)} \quad A.$$

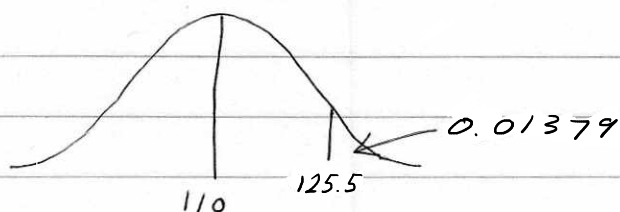
$$c) \quad P(X < 8) = \underline{\underline{0.0435}} \text{ (3sf)}$$

$$\begin{aligned} d) \quad & \frac{0.0468 - 0.0435}{0.0435} \times 100 \\ &= \underline{\underline{7.45\%}} \text{ 3sf} \end{aligned}$$

2a) They would have no light bulbs left to sell.

$$b/ \quad H_0: p = 55\% \\ H_1: p > 55\%$$

$$c/ \quad \begin{aligned} \mu &= np \\ &= 200(0.55) \\ &= 110 \end{aligned} \quad \begin{aligned} \sigma^2 &= np(1-p) \\ &= 200(0.55)(0.45) \\ &= 49.5 \\ \sigma &= \sqrt{49.5} \end{aligned}$$



$$126 \quad \begin{aligned} \text{LB} &= 125.5 \\ \text{UB} &= 126.5 \end{aligned}$$

$0.01379 < 0.05 \therefore$ we can reject H_0 and accept H_1 . The manufacturer's claim is justified.

$$3a/ \quad \begin{aligned} \mu &= np \\ &= 50(0.6) \\ &= 30 \end{aligned} \quad \begin{aligned} \sigma^2 &= np(1-p) \\ &= 50(0.6)(0.4) \\ &= 12 \\ \sigma &= \sqrt{12} \end{aligned}$$

$$\begin{aligned} 26 &: \text{upper bound } 26.5 \\ &\text{lower bound } 25.5 \end{aligned}$$

$$P(25.5 < X < 26.5) = 0.0592 \quad (3st)$$

b) There is not enough evidence to say that Andy's claim is incorrect.
There is a 5.92% chance of him getting 26 serves in if his claim is correct.

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$$\begin{aligned}\mu &= np \\ &= n(0.38) \\ &= 0.38n\end{aligned}$$

$$\begin{aligned}\sigma^2 &= np(1-p) \\ &= n(0.38)(0.62) \\ &= 0.2356n \\ \sigma &= \sqrt{0.2356n}\end{aligned}$$

$$P(X > 65.5) = 0.0438$$

$$1 - 0.0438 = 0.9562$$

[Inverse Normal] $\mu = 0$ $\sigma = 1$

$$z = 1.708 \dots$$

$$1.708 = \frac{65.5 - 0.38n}{\sqrt{0.2356n}}$$

$$1.708(\sqrt{0.2356n}) = 65.5 - 0.38n$$

$$0.38n + 0.829n^{\frac{1}{2}} - 65.5 = 0$$

$$n^{\frac{1}{2}} = \frac{-0.829 \pm \sqrt{(0.829)^2 - 4(0.38)(-65.5)}}{2(0.38)}$$

$$n^{\frac{1}{2}} = 12.08 \dots \quad \text{or} \quad n^{\frac{1}{2}} = -14. \dots$$

$$\underline{\underline{n = 146}}$$

~~$$n = 203$$~~

$\sqrt{n} \neq$ negative number.