

$$1a) \quad \cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos A = \frac{(6)^2 + (6)^2 - (8)^2}{2(6)(6)}$$

$$\cos A = \frac{1}{9}$$

$$A = \cos^{-1}\left(\frac{1}{9}\right)$$

$$= 1.459^\circ \text{ (3dp)}$$

$$b) \quad \text{Sector Area} = \frac{\theta}{2} r^2$$

$$= \frac{1.459}{2} (6)^2$$

$$= 26.3 \text{ cm}^2 \text{ (3sf)}$$

$$c) \quad \text{Triangle Area} = \frac{1}{2} ab \sin C$$

$$= \frac{1}{2} (6)(6) \sin(1.459)$$

$$= 17.9 \text{ cm}^2 \text{ (3sf)}$$

$$\text{Shaded Area} = "26.3" - "17.9"$$

$$= 8.38 \text{ cm}^2 \text{ (3sf)} \quad \left[\text{using all digits in whole number calculator} \right]$$

$$\begin{aligned} 2a) \quad \text{Arc Length} &= \theta \times r \\ &= 0.5 \times 5 \\ &= \underline{\underline{2.5 \text{ m}}} \end{aligned}$$

$$\begin{aligned} b) \quad \text{Sector Area} &= \frac{\theta}{2} r^2 \\ &= \frac{25}{4} \text{ m}^2 \end{aligned}$$

c) Length BM

$$BM^2 = (5)^2 + (2.5)^2 - 2(5)(2.5) \cos(0.5)$$

$$BM^2 = 9.3104 \dots$$

$$BM = 3.05 \text{ m (3sf)}$$

$$\begin{aligned} \text{Perimeter} &= 2.5 + 2.5 + 3.05 \\ &= 8.05 \text{ m (3sf)} \end{aligned}$$

d) Shaded region = Sector Area - Triangle Area

$$\text{Triangle Area} = \frac{1}{2} (2.5)(5) \sin(0.5)$$

$$= 2.996 \text{ m}^2$$

$$\text{Shaded Area} = \frac{25}{4} - 2.996$$

$$= \underline{\underline{3.25 \text{ m}^2}} \text{ (3sf)}$$

$$\begin{aligned} 3a) \quad \text{Arc Length} &= r\theta \\ &= 7(0.6) \\ &= 4.2 \text{ cm} \end{aligned}$$

$$\begin{aligned} b) \quad \text{Sector Area} &= \frac{\theta}{2} r^2 \\ &= \frac{0.6}{2} (7)^2 \\ &= 14.7 \text{ cm}^2 \end{aligned}$$

$$c) \quad \frac{\pi}{2} - 0.6 = \underline{\underline{0.971}}^\circ \text{ (3sf)}$$

$$\begin{aligned} d) \quad \text{Triangle Area} &= \frac{1}{2} (5)(7) \sin(0.971) \\ &= 14.4 \text{ cm}^2 \text{ (3sf)} \end{aligned}$$

$$\begin{aligned} \text{Total Area} &= 14.7 + 14.4 \\ &= \underline{\underline{29.1 \text{ cm}^2}} \text{ (3sf)} \end{aligned}$$