

Write your name here

Surname

Other Names

Mathematics

Practice Set A Paper 3 (Calculator) Higher Tier

Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
– there may be more space than you need.
- **Calculators may be used.**
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must **show all your working out.**



Information

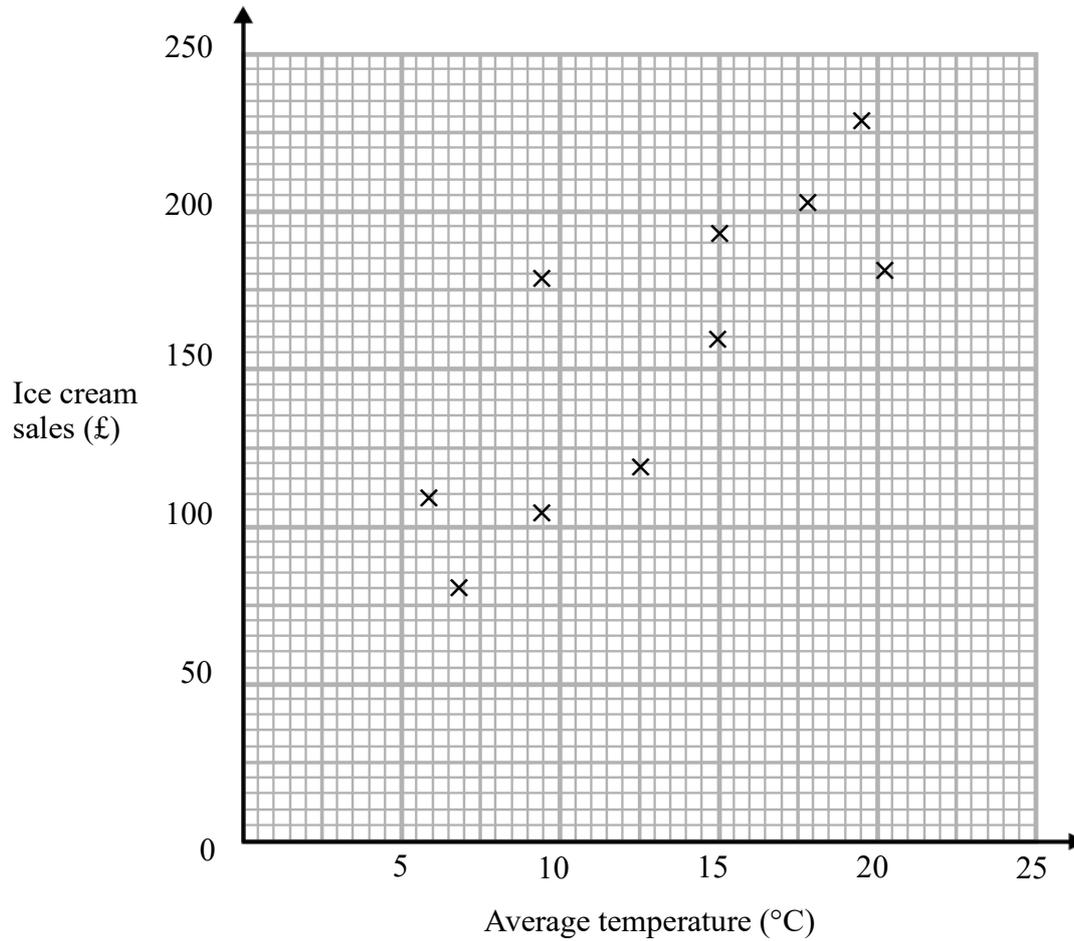
- The total mark for this paper is 80
- The marks for **each** question are shown in brackets
– use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

- 1 The average daytime temperature for 10 days is recorded.
A shop also records its ice cream sales for each of the 10 days.

The scatter graph shows this information.



- (a) What type of correlation does the scatter graph show?

..... (1)

- (b) On the 11th day the temperature was 12°. Estimate the ice cream sales on the 11th day.

..... (2)

- (c) The shop's manager wants to use the scatter graph to predict the ice cream sales for a day with an average temperature of 2°. Comment on the reliability of this prediction.

.....

 (1)

(Total for Question 1 is 4 marks)

2 Solve $8t - 19 = 5t - 11$

$t =$ _____

(Total for Question 2 is 2 marks)

3 Bob is going to make some orange paint.
He needs to mix red paint, yellow paint and white paint in the ratio 7 : 6 : 2

Bob wants to make 750 ml of orange paint.

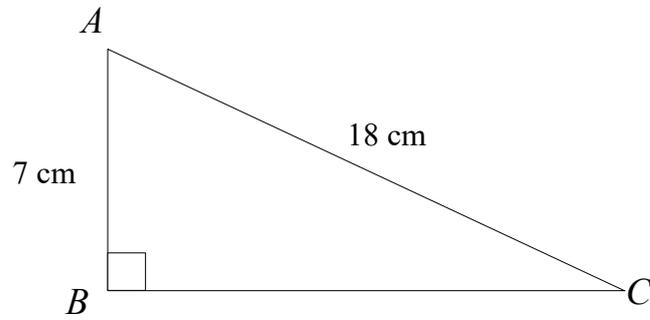
Bob has

400 ml of red paint
300 ml of yellow paint
200 ml of white paint

Does Bob have enough red paint, yellow paint and white paint to make the orange paint?
You must show all your working.

(Total for Question 3 is 4 marks)

5



Calculate the size of angle ACB .

.....°

(Total for Question 5 is 2 marks)

6 (a) Factorise fully $18a^2b + 12ab^2$

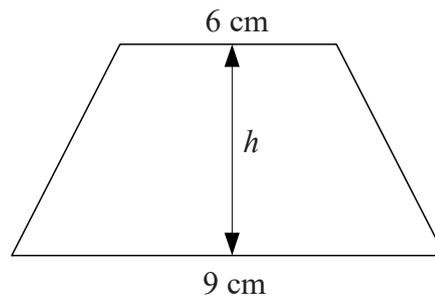
(b) Expand and Simplify $5(2y - 5) - 3(2y - 1)$

.....
(2)

.....
(2)

(Total for Question 6 is 4 marks)

- 7 The diagram shows a trapezium with an area of 45 cm^2 and a perpendicular height h cm.



Find the value of h .

$h =$

(Total for Question 7 is 2 marks)

- 8 (a) Write 7.329×10^6 as an ordinary number.

(b) Write 0.0508 in standard form.

..... (1)

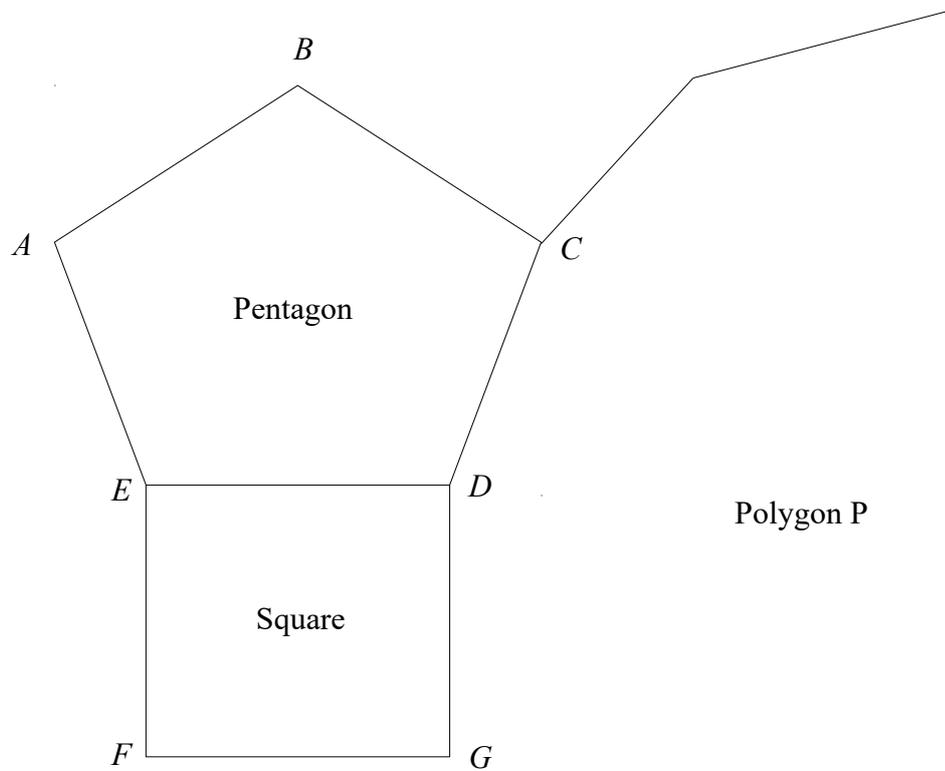
(c) Calculate $(5.51 \times 10^4) \div (5.8 \times 10^{-3})$
Give your answer in standard form.

..... (1)

..... (2)

(Total for Question 8 is 4 marks)

9



The diagram shows a regular pentagon, ABCDE, and a square, EDFG.

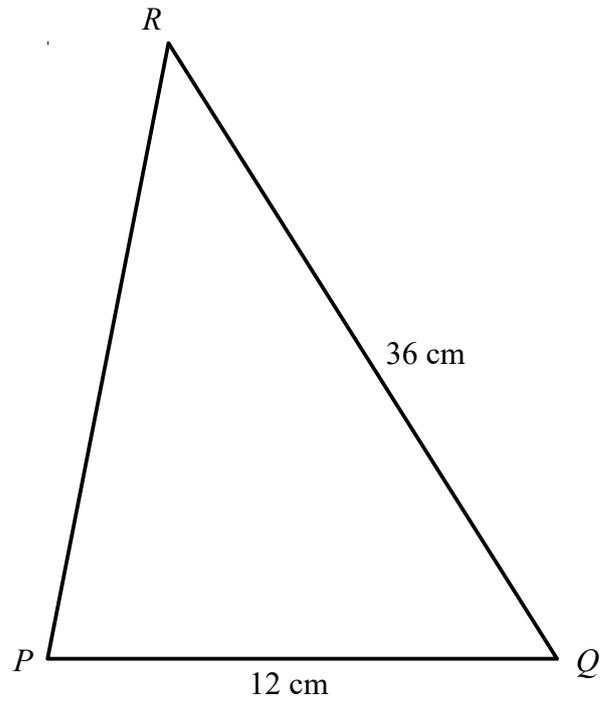
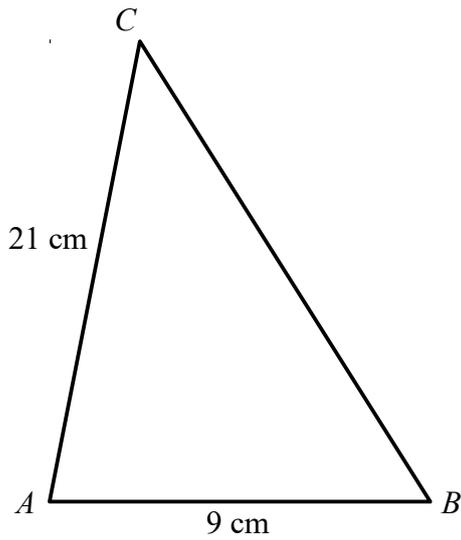
The lines CD and DG are both sides of another regular polygon, P.

How many sides does polygon P have?

You must show how you got your answer.

.....
(Total for Question 9 is 4 marks)

10



The two triangles ABC and PQR are mathematically similar.

Angle $A =$ angle P

Angle $B =$ angle Q

$AB = 9$ cm

$AC = 21$ cm

$PQ = 12$ cm

$QR = 36$ cm

(a) Calculate the length of PR .

..... cm
(2)

(b) Calculate the length of BC .

..... cm
(2)

(Total for Question 10 is 4 marks)

11 A population of bacteria is increasing by 12% each hour.

Find the percentage increase in the population every 3 hours.

.....
(Total for Question 11 is 2 marks)

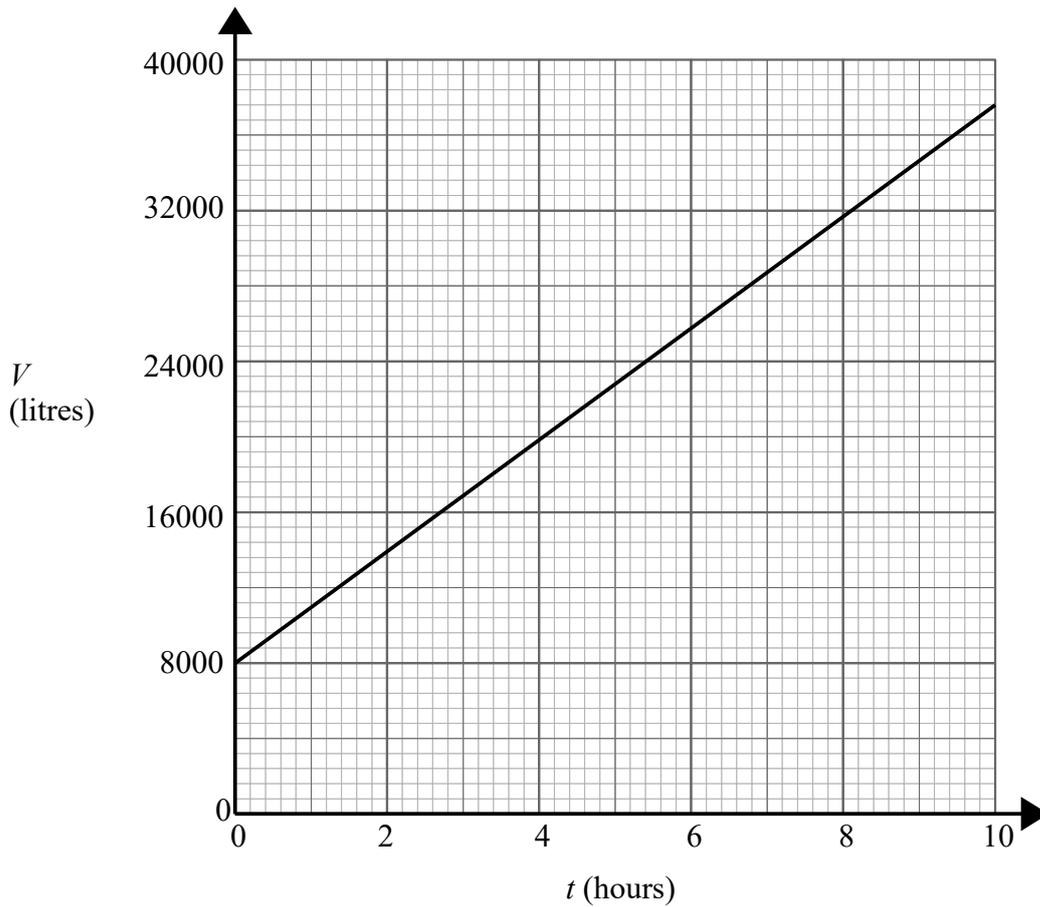
12 Light **A** flashes every 5 seconds.
Light **B** flashes every 6 seconds.
Light **C** flashes every 7 seconds.

All three lights flash at the same time.

How many times in one hour will the three lamps flash at the same time?

.....
(Total for Question 12 is 3 marks)

- 13 Bernie is filling up a swimming pool.
The graph shows the volume v of water in the swimming pool at time t hours.



Work out the rate of that the water is flowing into the pool.

Give your answer in litres per hour.

..... l/hr

(Total for Question 13 is 2 marks)

- 14** Cylinder A and cylinder B are mathematically similar.
The surface area of cylinder A is 50 cm^2 and the surface area of cylinder B is 128 cm^2
The volume of cylinder A is 80 cm^3
- Calculate the volume of cylinder B.

..... cm^3

(Total for Question 14 is 3 marks)

- 15** There are 12 people in a room.
Each person shakes each other person's hand once.
- Work out the number handshakes that take place.

.....
(Total for Question 15 is 2 marks)

- 16** By completing the square, find the coordinates of the turning point of the curve with the equation $y = x^2 - 3x + 1$
You must show all your working.

.....
(Total for Question 16 is 3 marks)

17 Here are the first 5 terms of a quadratic sequence.

6

10

17

27

40

Find an expression, in terms of n , for the n th term of this sequence.

.....
(Total for Question 17 is 4 marks)

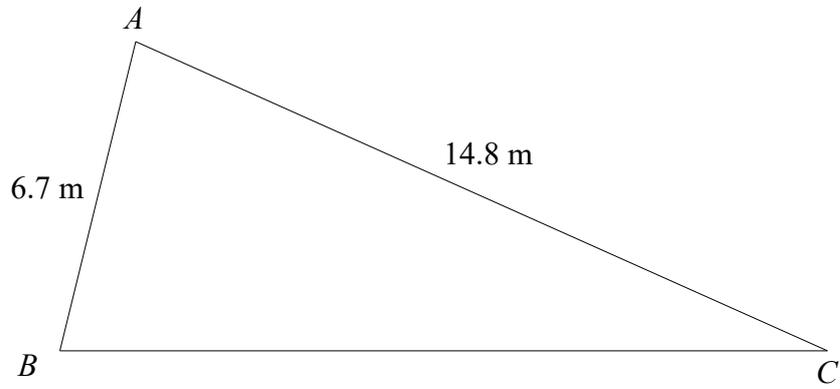
18 Given that

$$x + 9 : 5x - 1 = x + 7 : 2x - 3$$

Find the possible values of x .

.....
(Total for Question 18 is 4 marks)

19



Angle BAC is acute and the area of the triangle is 45 m^2
Calculate the perimeter of triangle ABC .
Give your answer to 3 significant figures.

.....m

(Total for Question 19 is 5 marks)

20 $ABCD$ is a parallelogram



Prove that triangle ABC and triangle BCD are congruent.

(Total for Question 20 is 3 marks)

21 (a) Show that the equation $x^3 + 4x = 1$ has a solution between $x = 0$ and $x = 1$.

(2)

(b) Show that the equation $x^3 + 4x = 1$ can be rearranged to give: $x = \frac{1}{4} - \frac{x^3}{4}$

(1)

(c) Starting with $x_0 = 0$, use the iteration formula $x_{n+1} = \frac{1}{4} - \frac{x_n^3}{4}$ twice to find an estimate for the solution to $x^3 + 4x = 1$

.....
(3)

(Total for Question 21 is 6 marks)

22 50 people were asked which fruits they liked from apples, bananas and oranges.

12 people like all three fruits.

34 people like apples.

7 like apples and bananas but not oranges.

16 like bananas and oranges.

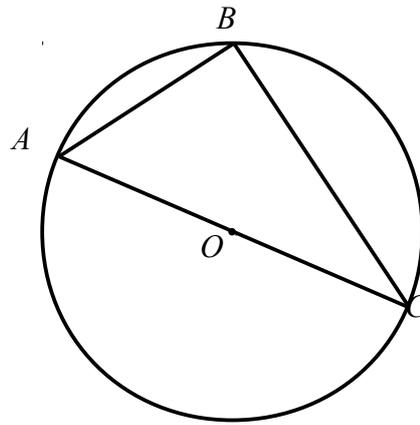
4 of the people do not like any of the fruits.

All 25 people who like oranges like at least one other fruit.

Two of the 50 people are chosen at random.

Work out the probability that they both like bananas.

.....
(Total for Question 22 is 5 marks)



A , B and C are points on the circumference of a circle, centre O .
 AOC is a diameter of the circle.

Prove that angle ABC is 90°
You must **not** use any circle theorems in your proof.