

Name: _____

IGCSE

Sequences

Instructions

- Use **black** ink or ball-point pen.
- Answer all Questions.
- Answer the Questions in the spaces provided
– *there may be more space than you need.*
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must **show all your working out.**

Information

- The marks for each Question are shown in brackets
– *use this as a guide as to how much time to spend on each Question.*

Advice

- Read each Question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every Question.
- Check your answers if you have time at the end

1 Here are the first five terms of a sequence.

2 5 8 11 14

Write down the next two terms in the sequence.

..... 17 , 20
(Total for Question 1 is 1 mark)

2 The first term in a sequence is 3.
The term to term rule is add 5.

3, 8, 13, 18, 23...

Is 97 a term in the sequence?
Give a reason for your answer.

No. All terms end in 3 and 8.

(Total for Question 2 is 2 marks)

3 Here are the first five terms of a sequence

6 10 14 18 22

Write down the next two terms in the sequence.

..... 26 , 30
(Total for Question 3 is 2 marks)

4 The n th term of a sequence is $4n + 3$

$$4(1) + 3 = 7$$

(a) Find the first two terms of this sequence.

$$4(2) + 3 = 11$$

..... 7 , 11

(b) Is 35 a term in this sequence.
You must show how you get your answer.

$$\begin{aligned} 4n + 3 &= 35 \\ 4n &= 32 \\ n &= 8 \end{aligned}$$

Yes, it is the 8th term.

(Total for Question 4 is 2 marks)

5 The n th term of a sequence is $n^2 + 1$

$$(1)^2 + 1 = 2$$

(a) Find the first two terms of this sequence.

$$(2)^2 + 1 = 5$$

..... 2 5
(1)

(b) Is 35 a term in this sequence.
You must show how you get your answer.

$$n^2 + 1 = 35$$

$$n^2 = 34$$

$$n = \sqrt{34} \text{ (not a whole number)}$$

No.....
.....
(1)

(Total for Question 5 is 2 marks)

6 Here are the first 5 terms of a sequence.

17 14 11 8 5

(a) Find the next term of this sequence.

..... 2
(1)

The n th term of a different sequence is $10n^2 + 5$

(b) Work out the 5th term of this sequence.

$$10(5)^2 + 5$$

$$10(25) + 5$$

$$250 + 5$$

..... 255
(1)

(Total for Question 6 is 2 marks)

7 Here are the first four terms of a sequence.

7 13 19 25

(a) Write down the next term in the sequence.

..... 31
(1)

(b) Explain how you got your answer

..... I added 6 to the previous term
(1)

(Total for Question 7 is 2 marks)

8 Here are the first four terms of a number sequence.

2 3 5 9

The rule to continue the sequence is
multiply the previous term by 2 and then subtract 1

Work out the 5th term of this sequence.

$$9 \times 2 = 18$$

$$18 - 1 = 17$$

..... 17

(Total for Question 8 is 1 mark)

9 Here are the first 5 terms of a sequence.

29 24 19 14 9

Find the 8th term of this sequence.

4 -1 -6

..... -6

(Total for Question 9 is 2 marks)

10 The n th term of a sequence is $n^2 + 3$

(a) Find the first three terms of this sequence.

$$(1)^2 + 3 = 4$$

$$(2)^2 + 3 = 7$$

$$(3)^2 + 3 = 12$$

..... 4 , 7 , 12
(2)

(b) Find the 10th term in this sequence.

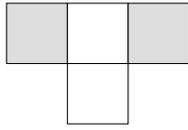
$$(10)^2 + 3 = 103$$

..... 103

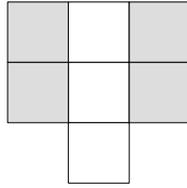
(1)

(Total for Question 10 is 3 marks)

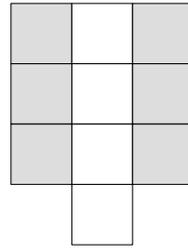
11 Here is a sequence of patterns made from white tiles and grey tiles.



pattern number 1

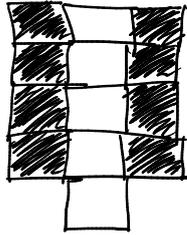


pattern number 2



pattern number 3

(a) In the space below, draw pattern number 4.



(1)

(b) Work out the total number of tiles to make pattern number 7.

4 7 10 13 16 19 22

..... 22

(2)

Kyle says

“There are 4 white tiles in pattern number 3 so there will be 8 white tiles in pattern number 6.”

(c) Is Kyle right?

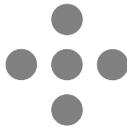
You must give a reason for your answer.

No. The number of white tiles goes up by 1 each time. There will be 7 white tiles in pattern 6.

(1)

(Total for Question 11 is 4 marks)

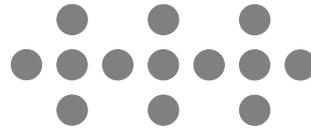
12 Here is a sequence of patterns made from grey counters.



pattern number 1

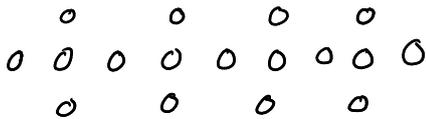


pattern number 2



pattern number 3

(a) In the space below, draw pattern number 4.



(b) Work out the total number of counters to make pattern number 10.

$$\begin{array}{cccccc} 4n+1 & 5 & 9 & 13 & 17 \\ 4n & 4 & 8 & 12 & 16 \end{array}$$

$$4n + 1$$

$$4(10) + 1 = 41$$

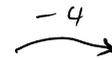
41

.....
(2)

(Total for Question 12 is 3 marks)

13 Here are the first five terms of a sequence.

31 27 23 19 15 11 7 3



(a) Find the first negative term in the sequence.

$$\begin{array}{cccc} -4n & -4 & -8 & -12 \\ -4n + 35 & 31 & 27 & 23 \end{array}$$

-1

.....
(2)

(b) Is -30 a term in this sequence?
Give a reason for your answer.

No. All terms in the sequence are odd.

.....
(1)

(Total for Question 13 is 3 marks)

14 Here are the first 5 terms of an arithmetic sequence.

-3 1 5 9 13

(a) Find an expression, in terms of n , for the n th term of this sequence.

$4n$ 4 8 12 16

$$\frac{4n - 7}{\dots\dots\dots} \quad (2)$$

The n th term of a different arithmetic sequence is $2n - 3$

(b) Is 101 a term in this sequence?
Show how you get your answer.

$$2n - 3 = 101$$

$$2n = 104$$

$$n = 52$$

Yes

52nd term

(2)

(Total for Question 14 is 4 marks)

15 Here are the first 5 terms of a sequence.

9 14 19 24 29

Find an expression, in terms of n , for the n th term of this sequence.

$5n$ 5 10 15 20

$$\frac{5n + 4}{\dots\dots\dots}$$

(Total for Question 15 is 2 marks)

16 Here are the first 5 terms of a sequence.

25 22 19 16 13

Find an expression, in terms of n , for the n th term of this sequence.

$-3n$ -3 -6 -9

$$\frac{-3n + 28}{\dots\dots\dots}$$

(Total for Question 16 is 2 marks)

17 Here are the first four terms of an arithmetic sequence.

4 11 18 25

Write down an expression, in terms of n , for the n th term of the sequence.

$7n$ 7 14 21 28

..... $7n - 3$

(Total for Question 17 is 2 marks)

18 Here are the first four terms of an arithmetic sequence.

35 31 27 23

Write down an expression, in terms of n , for the n th term of the sequence.

$-4n$ -4 -8 -12 -16

..... $-4n + 39$

(Total for Question 18 is 2 marks)

19 Here are the first five terms of an arithmetic sequence.

21 27 33 39 45

Write down an expression, in terms of n , for the n th term of the sequence.

$6n$ 6 12 18 24 30

..... $6n + 15$

(Total for Question 19 is 2 marks)

20 Here are the first five terms of an arithmetic sequence.

2 7 12 17 22

Write down an expression, in terms of n , for the n th term of the sequence.

$5n$ 5 10 15 20 25

..... $5n - 3$

(Total for Question 20 is 2 marks)