

Negative and Fractional Indices

If a power is negative
we flip the answer:

$$2^{-1} = \frac{1}{2} \quad 3^{-2} = \frac{1}{9} \quad 5^{-1} = \frac{1}{5}$$

$$\left(\frac{3}{4}\right)^{-1} = \frac{4}{3} \quad 5^{-2} = \frac{1}{25} \quad \left(\frac{2}{5}\right)^{-1} = \frac{5}{2}$$

This is because:

$$2^3 \div 2^5 = 2^{-2}$$

We know this is true from the earlier rules

$$2^3 \text{ is } 8 \text{ and } 2^5 \text{ is } 32$$

$$8 \div 32 = \frac{1}{4}$$

$$\text{So } 2^{-2} = \frac{1}{4}$$

Power of $\frac{1}{2}$ means
square root

$$49^{\frac{1}{2}} = 7 \quad 4^{\frac{1}{2}} = 2 \quad 100^{\frac{1}{2}} = 10$$

$$25^{\frac{1}{2}} = 5 \quad 9^{\frac{1}{2}} = 3$$

This is because:

$$9^{\frac{1}{2}} \times 9^{\frac{1}{2}} = 9^1$$

We know this is true from the earlier rules

$$3 \times 3 = 9$$

$$\text{So } 9^{\frac{1}{2}} = 3$$