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Centre No.				Pape	er Refer	ence			Surname	Initial(s)
Candidate No.		6	6	6	6	/	0	1	Signature	

Paper Reference(s)

# 6666/01

# **Edexcel GCE**

# **Core Mathematics C4 Advanced**

Wednesday 25 January 2012 - Afternoon

Time: 1 hour 30 minutes

Materials required for examination Mathematical Formulae (Pink) Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

#### **Instructions to Candidates**

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer for each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

#### **Information for Candidates**

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 8 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

#### **Advice to Candidates**

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

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8

Examiner's use only

Team Leader's use only

Question Number

1

2

3

4

5

6

Turn over

Total

**PEARSON** 

W850/R6665/57570 5/4/5

The curve C has the equation  $2x + 3y^2 + 3x^2y = 4x^2$ . The point P on the curve has coordinates (-1, 1).

(a) Find the gradient of the curve at P.

(5)

(b) Hence find the equation of the normal to C at P, giving your answer in the form ax+by+c=0, where a, b and c are integers.

> $u = 3x^{2} \quad v = y$   $\frac{du}{dx} = 6x \quad \frac{dv}{dx} = \frac{dy}{dx}$ (3)

+ 6 y dy + 6 sey + 3 set dy = 8 se

9 dy

4y = 9x +13

9x -4y +13 =0

2. (a) Use integration by parts to find  $\int x \sin 3x \, dx$ .

(3)

(b) Using your answer to part (a), find  $\int x^2 \cos 3x \, dx$ .

(3)

u dv dx = uv - v dy dx

u = oc dv = sin 300

 $\frac{du}{dx} = 1 \qquad v = -\frac{1}{3}\cos 3x$ 

= -\frac{1}{3} \times \cos 3 \times - \frac{1}{3} \cos 3 \times \dot

= - 3x cos 3x - [- g sin 3x] + c

= - \frac{1}{3} \pi (053) \pi + \frac{1}{9} \sin 3 \pi + C

 $u = 3c^{2} \frac{dv}{dx} = \cos 3x$   $\frac{du}{dx} = 2x \quad v = \frac{1}{3} \sin 3x$ 

= 3x sin3x - = = x sin3x dac

= 3x2 Sin 3x + 2 2 cos 3x - 27 sin3x+C

# 3. (a) Expand

$$\frac{1}{(2-5x)^2}$$
,  $|x| < \frac{2}{5}$ 

in ascending powers of x, up to and including the term in  $x^2$ , giving each term as a simplified fraction.

(5)

Given that the binomial expansion of  $\frac{2 + kx}{(2-5x)^2}$ ,  $|x| < \frac{2}{5}$ , is

$$\frac{1}{2} + \frac{7}{4}x + Ax^2 + \dots$$

(b) find the value of the constant k,

(2)

(c) find the value of the constant A.

(2)

a) 
$$(2-5\infty)^{-2}$$

$$\frac{1 + nx + n(n-1)x^2}{2}$$

$$2^{-2}(1-\frac{5}{2}x)^{-2}$$

$$\frac{1}{4}\left(1-\frac{5}{2}c\right)^{-2}$$

$$\frac{1}{4}\left(1+(-2)(-\frac{5}{2}x)+(-2)(-\frac{5}{3})(-\frac{5}{2}x)\right)^{2}$$

$$\frac{1}{4}(1+5x+\frac{75}{4}x^2)$$

$$\frac{1}{4} + \frac{5}{4}x + \frac{75}{16}x^2$$

$$\infty$$
 coefficient:  $\frac{5}{42} + \frac{1}{4}k = \frac{7}{4}$ 

$$\frac{1}{4}k = \frac{-3}{4}$$

# Question 3 continued

$$\frac{75}{8} + \frac{5}{4}(-3) = A$$



Leave blank

4.

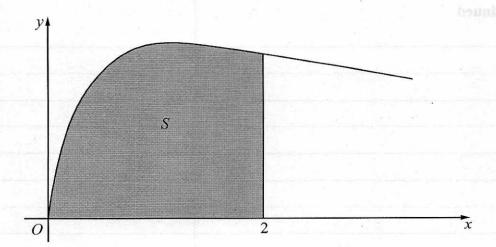


Figure 1

Figure 1 shows the curve with equation

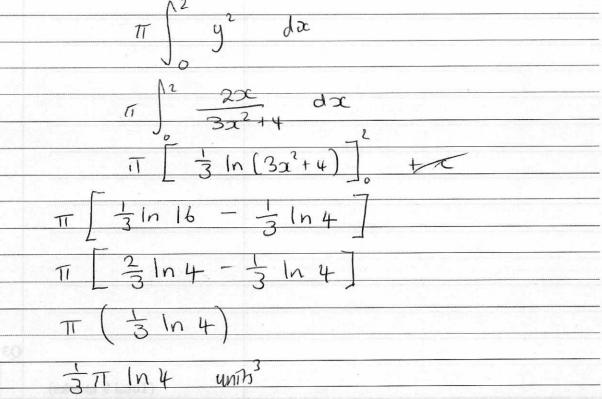
$$y = \sqrt{\left(\frac{2x}{3x^2 + 4}\right)}, \ x \geqslant 0$$

The finite region S, shown shaded in Figure 1, is bounded by the curve, the x-axis and the line x = 2

The region S is rotated 360° about the x-axis.

Use integration to find the exact value of the volume of the solid generated, giving your answer in the form  $k \ln a$ , where k and a are constants.

(5)



5.

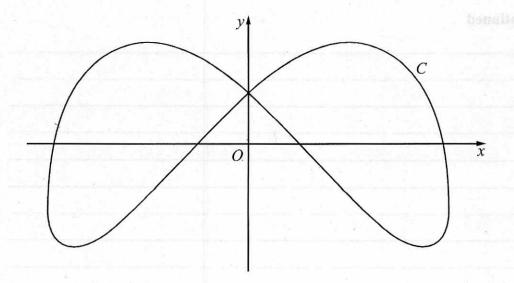


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = 4\sin\left(t + \frac{\pi}{6}\right), \quad y = 3\cos 2t, \quad 0 \leqslant t < 2\pi$$

(a) Find an expression for  $\frac{dy}{dx}$  in terms of t.

(3)

Leave blank

(b) Find the coordinates of all the points on C where  $\frac{dy}{dx} = 0$ 

(5)

a) 
$$\frac{doc}{dt} = 4 \cos(t + \frac{\pi}{6}) \frac{dy}{dt} = -\frac{2}{3} \sin 2t$$

$$\frac{dy}{dx} = \frac{dy}{dt} = \frac{-2/3 \sin 2t}{4 \cos 3(t + 1)/6}$$

$$\frac{-2/3 \sin 2t}{4 \cos (t+T/8)} = 0$$

$$-\frac{2}{3}\sin 2t = 0$$

$$\sin 2t = 0$$

$$2t = 0, \pi, 2\pi, 3\pi$$

$$t = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$$

Question	5	continued

E=0	(2,3)
t= 11/2	$(2\sqrt{3}, -3)$
t=TT	(-2,3)
t = 35	$(-2\sqrt{3}, -3)$
	( ) ()



6.



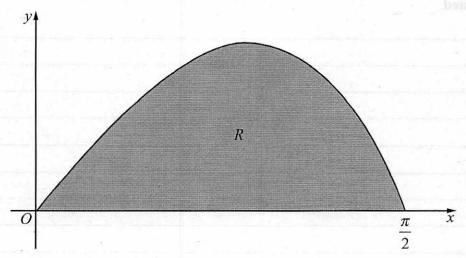


Figure 3

Figure 3 shows a sketch of the curve with equation  $y = \frac{2\sin 2x}{(1+\cos x)}$ ,  $0 \le x \le \frac{\pi}{2}$ .

The finite region R, shown shaded in Figure 3, is bounded by the curve and the x-axis.

The table below shows corresponding values of x and y for  $y = \frac{2\sin 2x}{(1+\cos x)}$ .

x	0	$\frac{\pi}{8}$	$\frac{\pi}{4}$	$\frac{3\pi}{8}$	$\frac{\pi}{2}$
y	0	0.73508	1.17157	1.02280	0

(a) Complete the table above giving the missing value of y to 5 decimal places.

(1)

(b) Use the trapezium rule, with all the values of y in the completed table, to obtain an estimate for the area of R, giving your answer to 4 decimal places.

(3)

(c) Using the substitution  $u = 1 + \cos x$ , or otherwise, show that

$$\int \frac{2\sin 2x}{(1+\cos x)} \, dx = 4\ln(1+\cos x) - 4\cos x + k$$

where k is a constant.

(5)

(d) Hence calculate the error of the estimate in part (b), giving your answer to 2 significant figures.

(3)

### Question 6 continued

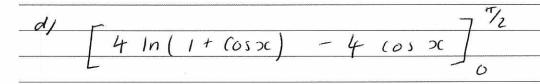
$$\frac{1}{8} \left( 0.73508 + 1.17157 + 1.02280 \right)$$

$$\int -4(u-1) du$$

$$-4(1+\cos x) + 4\ln(1+\cos x) + c$$
  
 $-4 - 4\cos x + 4\ln(1+\cos x) + c$   
 $-4\ln(1+\cos x) - 4\cos x + k$ 

Question	& continued
Question	p continued

6



7. Relative to a fixed origin O, the point A has position vector  $(2\mathbf{i} - \mathbf{j} + 5\mathbf{k})$ , the point B has position vector  $(5\mathbf{i} + 2\mathbf{j} + 10\mathbf{k})$ , and the point D has position vector  $(-\mathbf{i} + \mathbf{j} + 4\mathbf{k})$ .

The line l passes through the points A and B.

(a) Find the vector  $\overrightarrow{AB}$ .

**(2)** 

(b) Find a vector equation for the line l.

(2)

(c) Show that the size of the angle BAD is 109°, to the nearest degree.

(4)

The points A, B and D, together with a point C, are the vertices of the parallelogram  $\overrightarrow{ABCD}$ , where  $\overrightarrow{AB} = \overrightarrow{DC}$ .

(d) Find the position vector of C.

(2)

(e) Find the area of the parallelogram ABCD, giving your answer to 3 significant figures.

(3)

(f) Find the shortest distance from the point D to the line l, giving your answer to 3 significant figures.

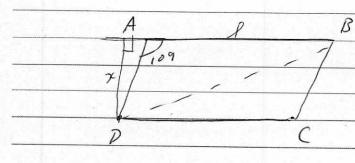
(2)

$$b/2i-j+5k+t(3i+3j+5k)$$

$$\sqrt{3^2+3^2+5^2}\sqrt{3^2+2^2+1^2}$$

(neavest degree

# Question 7 continued



$$d/. C = (-i+j+4k) + (3:+3j+5k)$$
= 2: +45+04

1 1777	Sin
77)	$Sin$ $Cos$ $(7) = \infty$
x /514	174
	3-(14 GO) 71
	- 122 crats
	= 3.54 units (3sf)

**8.** (a) Express  $\frac{1}{P(5-P)}$  in partial fractions.

(3)

A team of conservationists is studying the population of meerkats on a nature reserve. The population is modelled by the differential equation

$$\frac{\mathrm{d}P}{\mathrm{d}t} = \frac{1}{15}P(5-P), \quad t \geqslant 0$$

where P, in thousands, is the population of meerkats and t is the time measured in years since the study began.

Given that when t = 0, P = 1,

(b) solve the differential equation, giving your answer in the form,

$$P = \frac{a}{b + c e^{-\frac{1}{3}t}}$$

where a, b and c are integers.

(8)

(c) Hence show that the population cannot exceed 5000

(1)

$$\frac{ay}{p(s-p)} = \frac{A}{p} + \frac{b}{5-p}$$

by 
$$\int_{P(5-P)}^{1} dP = \int_{15}^{L} dt$$

## **Question 8 continued**

$$\int \frac{1}{5P} + \frac{1}{5(5-P)} dP = \int \frac{1}{15} dt$$

$$\frac{1}{5} \ln P - \frac{1}{5} \ln (5-P) = \frac{1}{15} + c$$

$$\frac{1}{5}\ln(1) - \frac{1}{5}\ln(4) = c$$

$$\frac{1}{5}\ln\left(\frac{4P}{5-P}\right) = \frac{1}{15}t$$

$$\ln \left(\frac{4P}{5-P}\right) = \frac{1}{3}t$$

$$4P = e^{3t}(5-P)$$

$$4P = 5e^{3t} - Pe^{3t}$$

$$4P + Pe^{3t} = 5e^{3t}$$

$$P(4 + e^{3t}) = 5e^{3t}$$

$$P = 5e^{3t}$$

$$4 + e^{3t}$$