



**1.**

$$y = 3^x + 2x$$

(a) Complete the table below, giving the values of  $y$  to 2 decimal places.

$x$	0	0.2	0.4	0.6	0.8	1
$y$	1	1.65				5

**(2)**

(b) Use the trapezium rule, with all the values of  $y$  from your table, to find an approximate

value for  $\int_0^1 (3^x + 2x) dx$ .

**(4)**


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**Question 3 continued**

Lined area for writing the answer to Question 3.

**Q3**

**(Total 4 marks)**



H 3 5 3 8 4 A 0 7 2 8



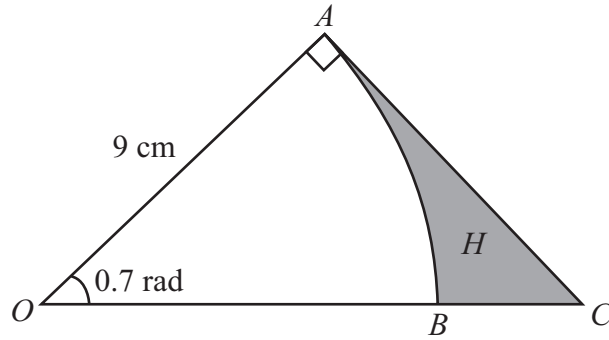








6.



**Figure 1**

Figure 1 shows the sector  $OAB$  of a circle with centre  $O$ , radius 9 cm and angle 0.7 radians.

- (a) Find the length of the arc  $AB$ . (2)
- (b) Find the area of the sector  $OAB$ . (2)

The line  $AC$  shown in Figure 1 is perpendicular to  $OA$ , and  $OBC$  is a straight line.

- (c) Find the length of  $AC$ , giving your answer to 2 decimal places. (2)

The region  $H$  is bounded by the arc  $AB$  and the lines  $AC$  and  $CB$ .

- (d) Find the area of  $H$ , giving your answer to 2 decimal places. (3)

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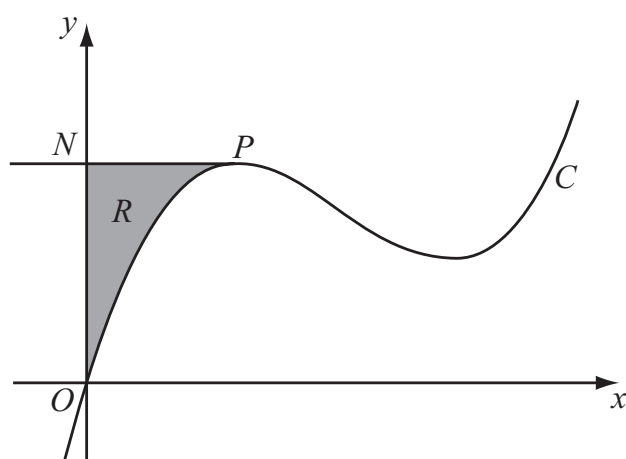








8.



**Figure 2**

Figure 2 shows a sketch of part of the curve  $C$  with equation

$$y = x^3 - 10x^2 + kx,$$

where  $k$  is a constant.

The point  $P$  on  $C$  is the maximum turning point.

Given that the  $x$ -coordinate of  $P$  is 2,

(a) show that  $k = 28$ .

**(3)**

The line through  $P$  parallel to the  $x$ -axis cuts the  $y$ -axis at the point  $N$ .  
The region  $R$  is bounded by  $C$ , the  $y$ -axis and  $PN$ , as shown shaded in Figure 2.

(b) Use calculus to find the exact area of  $R$ .

**(6)**

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**Question 8 continued**

Lined area for writing the answer to Question 8.

**(Total 9 marks)**

Q8



9. The adult population of a town is 25 000 at the end of Year 1.

A model predicts that the adult population of the town will increase by 3% each year, forming a geometric sequence.

(a) Show that the predicted adult population at the end of Year 2 is 25 750. (1)

(b) Write down the common ratio of the geometric sequence. (1)

The model predicts that Year  $N$  will be the first year in which the adult population of the town exceeds 40 000.

(c) Show that

$$(N-1)\log 1.03 > \log 1.6 \tag{3}$$

(d) Find the value of  $N$ . (2)

At the end of each year, each member of the adult population of the town will give £1 to a charity fund.

Assuming the population model,

(e) find the total amount that will be given to the charity fund for the 10 years from the end of Year 1 to the end of Year 10, giving your answer to the nearest £1000. (3)

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**Question 9 continued**

Lined area for writing the answer to Question 9.

**Q9**

**(Total 10 marks)**



10. The circle  $C$  has centre  $A(2, 1)$  and passes through the point  $B(10, 7)$ .

(a) Find an equation for  $C$ .

(4)

The line  $l_1$  is the tangent to  $C$  at the point  $B$ .

(b) Find an equation for  $l_1$ .

(4)

The line  $l_2$  is parallel to  $l_1$  and passes through the mid-point of  $AB$ .

Given that  $l_2$  intersects  $C$  at the points  $P$  and  $Q$ ,

(c) find the length of  $PQ$ , giving your answer in its simplest surd form.

(3)

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### Question 10 continued

*(This area contains 35 horizontal lines for writing.)*



