

- 1 Find the binomial expansion of each of the following in ascending powers of x up to and including the term in x^3 , for $|x| < 1$.
- a $(1+x)^{-1}$ b $(1+x)^{\frac{1}{2}}$ c $2(1+x)^{-3}$ d $(1+x)^{\frac{2}{3}}$
 e $\sqrt[3]{1-x}$ f $\frac{1}{(1+x)^2}$ g $\frac{1}{4(1-x)^4}$ h $\frac{3}{\sqrt{1-x}}$
- 2 Expand each of the following in ascending powers of x up to and including the term in x^3 and state the set of values of x for which each expansion is valid.
- a $(1+2x)^{\frac{1}{2}}$ b $(1-3x)^{-1}$ c $(1-4x)^{-\frac{1}{2}}$ d $(1+\frac{1}{2}x)^{-3}$
 e $(1-6x)^{\frac{1}{3}}$ f $(1+\frac{1}{4}x)^{-4}$ g $(1+2x)^{\frac{3}{2}}$ h $(1-3x)^{-\frac{4}{3}}$
- 3 a Expand $(1-2x)^{\frac{1}{2}}$, $|x| < \frac{1}{2}$, in ascending powers of x up to and including the term in x^3 .
 b By substituting a suitable value of x in your expansion, find an estimate for $\sqrt{0.98}$
 c Show that $\sqrt{0.98} = \frac{7}{10}\sqrt{2}$ and hence find the value of $\sqrt{2}$ correct to 8 significant figures.
- 4 Expand each of the following in ascending powers of x up to and including the term in x^3 and state the set of values of x for which each expansion is valid.
- a $(2+x)^{-1}$ b $(4+x)^{\frac{1}{2}}$ c $(3-x)^{-3}$ d $(9+3x)^{\frac{1}{2}}$
 e $(8-24x)^{\frac{1}{3}}$ f $(4-3x)^{-1}$ g $(4+6x)^{-\frac{1}{2}}$ h $(3+2x)^{-2}$
- 5 a Expand $(1+2x)^{-1}$, $|x| < \frac{1}{2}$, in ascending powers of x up to and including the term in x^3 .
 b Hence find the series expansion of $\frac{1-x}{1+2x}$, $|x| < \frac{1}{2}$, in ascending powers of x up to and including the term in x^3 .
- 6 Find the first four terms in the series expansion in ascending powers of x of each of the following and state the set of values of x for which each expansion is valid.
- a $\frac{1+3x}{1-x}$ b $\frac{2x-1}{(1+4x)^2}$ c $\frac{3+x}{2-x}$ d $\frac{1-x}{\sqrt{1+2x}}$
- 7 a Express $\frac{x-2}{(1-x)(1-2x)}$ in partial fractions.
 b Hence find the series expansion of $\frac{x-2}{(1-x)(1-2x)}$ in ascending powers of x up to and including the term in x^3 and state the set of values of x for which the expansion is valid.
- 8 By first expressing $f(x)$ in partial fractions, find the series expansion of $f(x)$ in ascending powers of x up to and including the term in x^3 and state the set of values of x for which it is valid.
- a $f(x) \equiv \frac{4}{(1+x)(1-3x)}$ b $f(x) \equiv \frac{1-6x}{1+3x-4x^2}$ c $f(x) \equiv \frac{5}{2-3x-2x^2}$
 d $f(x) \equiv \frac{7x-3}{x^2-4x+3}$ e $f(x) \equiv \frac{3+5x}{(1+3x)(1+x)^2}$ f $f(x) \equiv \frac{2x^2+4}{2x^2+x-1}$