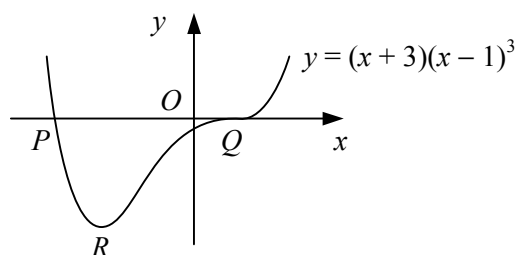


- 1 A curve has the equation $y = x^2(2 - x)^3$ and passes through the point $A(1, 1)$.
- Find an equation for the tangent to the curve at A .
 - Show that the normal to the curve at A passes through the origin.
- 2 A curve has the equation $y = \frac{x}{2x+3}$.
- Find an equation for the tangent to the curve at the point $P(-1, -1)$.
 - Find an equation for the normal to the curve at the origin, O .
 - Find the coordinates of the point where the tangent to the curve at P meets the normal to the curve at O .

3



The diagram shows the curve with equation $y = (x + 3)(x - 1)^3$ which crosses the x -axis at the points P and Q and has a minimum at the point R .

- Write down the coordinates of P and Q .
 - Find the coordinates of R .
- 4 Given that $y = x\sqrt{4x+1}$,
- show that $\frac{dy}{dx} = \frac{6x+1}{\sqrt{4x+1}}$,
 - solve the equation $\frac{dy}{dx} - 5y = 0$.
- 5 A curve has the equation $y = \frac{2(x-1)}{x^2+3}$ and crosses the x -axis at the point A .
- Show that the normal to the curve at A has the equation $y = 2 - 2x$.
 - Find the coordinates of any stationary points on the curve.
- 6 $f(x) \equiv x^{\frac{3}{2}}(x-3)^3, x > 0$.
- Show that $f'(x) = kx^{\frac{1}{2}}(x-1)(x-3)^2$, where k is a constant to be found.
 - Hence, find the coordinates of the stationary points of the curve $y = f(x)$.
- 7 $f(x) = x\sqrt{2x+12}, x \geq -6$.
- Find $f'(x)$ and show that $f''(x) = \frac{3(x+8)}{(2x+12)^{\frac{3}{2}}}$.
 - Find the coordinates of the turning point of the curve $y = f(x)$ and determine its nature.