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Surname

Other Names

Mathematics Paper 1 (Non-Calculator) Higher Tier

Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name,
- centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may not be used.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must show all your working out.

Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.



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Higher Tier Formulae Sheet

Perimeter, area and volume

Where a and b are the lengths of the parallel sides and h is their perpendicular separation:

Area of a trapezium =
$$\frac{1}{2}(a+b)h$$

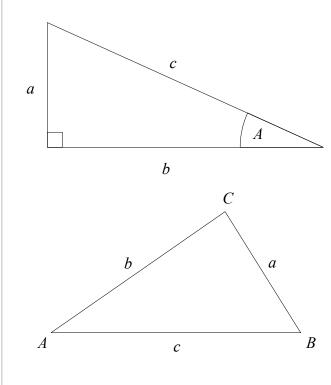
Volume of a prism = area of cross section \times length

Where r is the radius and d is the diameter:

Circumference of a circle = $2\pi r = \pi d$

Area of a circle = πr^2

Pythagoras' Theorem and Trigonometry



Compound Interest

Where P is the principal amount, r is the interest rate over a given period and n is number of times that the interest is compounded:

Total accrued =
$$P\left(1 + \frac{r}{100}\right)'$$

END OF EXAM AID

Quadratic formula

The solution of $ax^2 + bx + c = 0$

where $a \neq 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

In any right-angled triangle where a, b and c are the length of the sides and c is the hypotenuse:

 $a^2 + b^2 = c^2$

In any right-angled triangle ABC where a, b and c are the length of the sides and c is the hypotenuse:

$$\sin A = \frac{a}{c} \quad \cos A = \frac{b}{c} \quad \tan A = \frac{a}{b}$$

In any triangle ABC where a, b and c are the length of the sides:

sine rule:
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

cosine rule: $a^2 = b^2 + c^2 - 2bc \cos A$

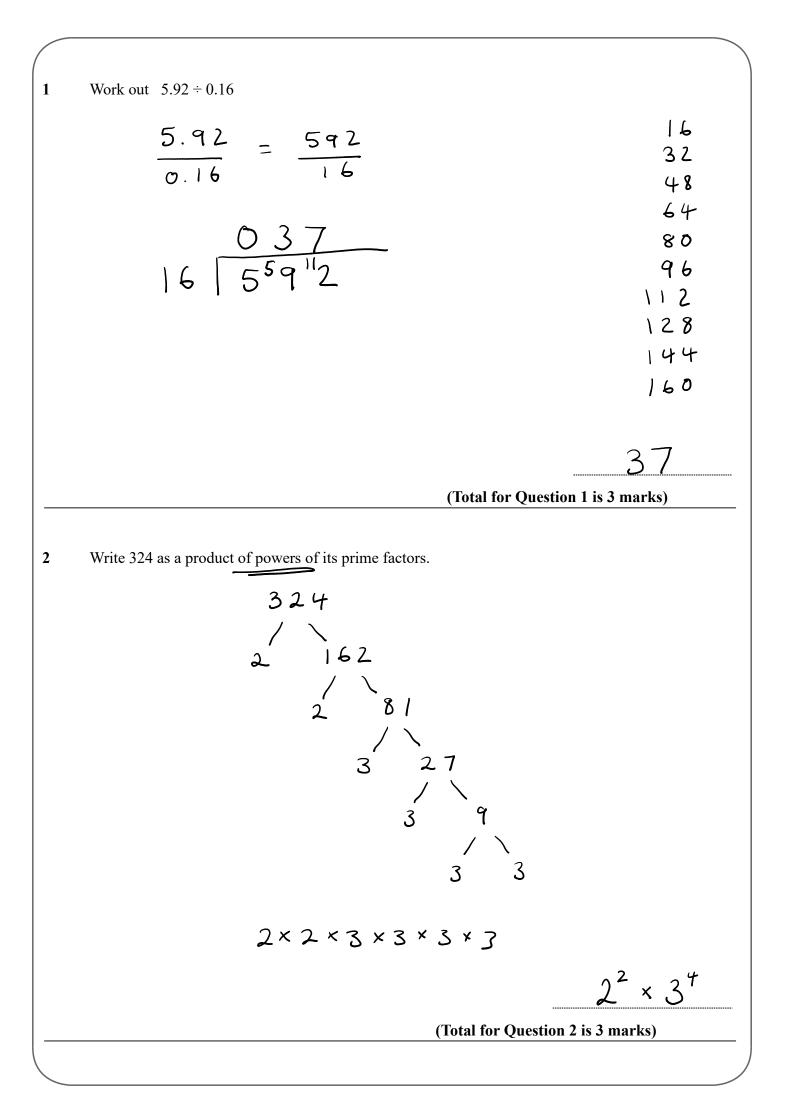
Area of triangle = $\frac{1}{2}ab\sin C$

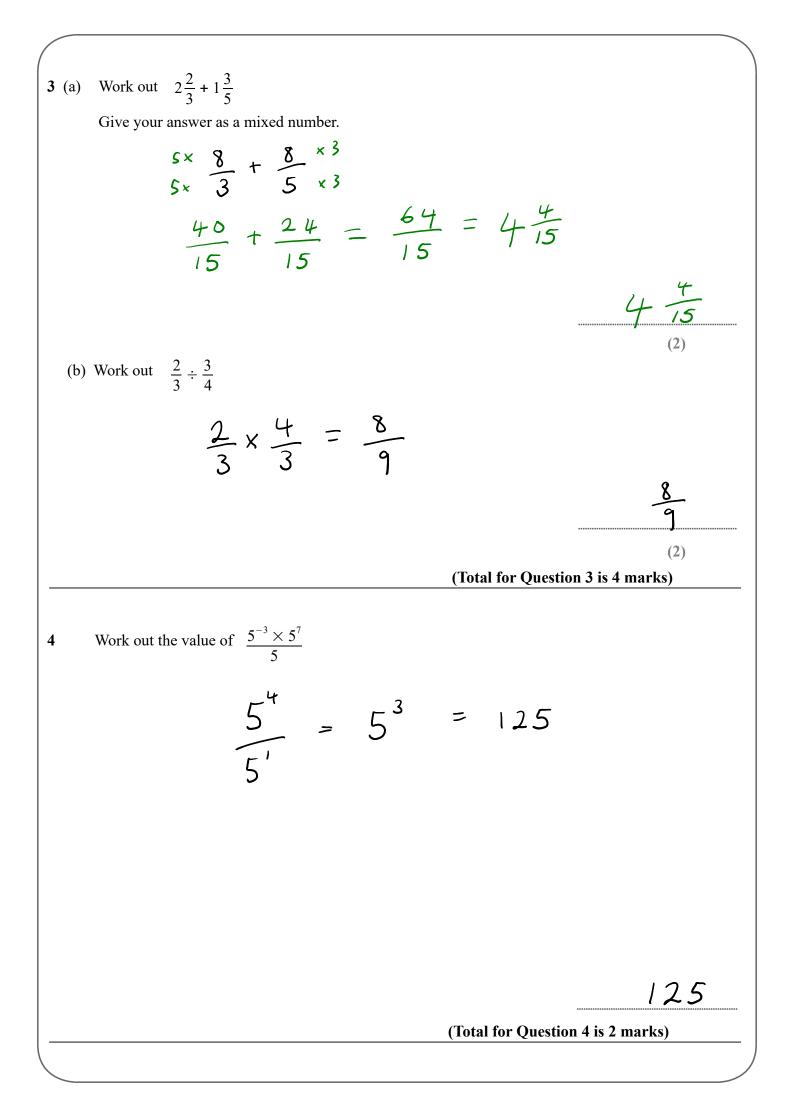
Probability

Where P(A) is the probability of outcome A and P(B) is the probability of outcome B:

P(A or B) = P(A) + P(B) - P(A and B)

$$P(A \text{ and } B) = P(A \text{ given } B) P(B)$$





Tracey writes down three numbers a, b and c.

$$a:b=3:5 \times 4$$

 $a:c=4:7 \times 3$

(a) Find a:b:c

12:20:21

(2)

Jamie writes down three numbers d, e and f.

d = 2ef = 3d

(b) Find e:d:f

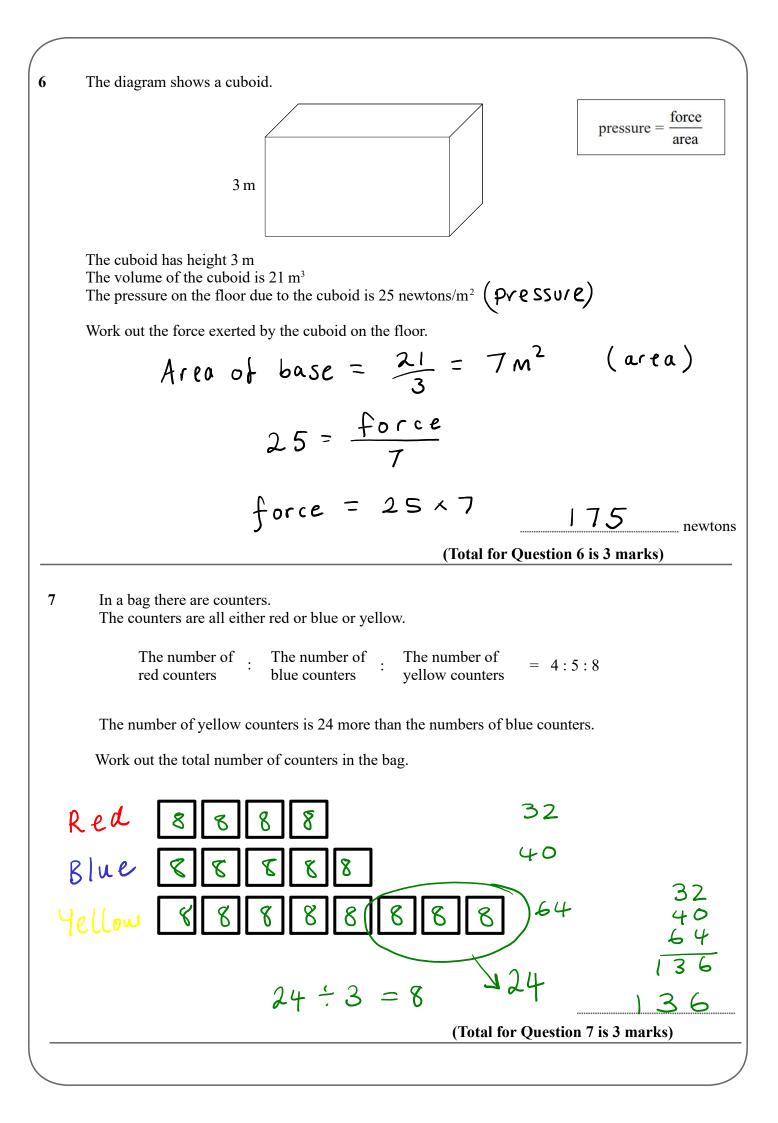
Let
$$e = 1$$

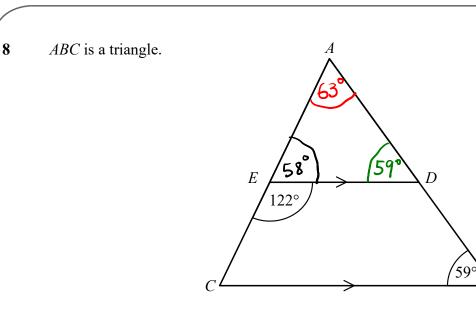
 $d = 2(1) = 2$
 $f = 3(2) = 6$

1:2:6

(2)

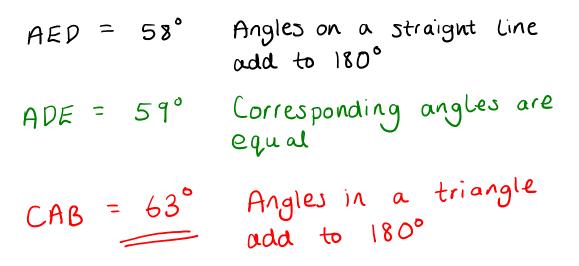
(Total for Question 5 is 4 marks)





AEC and ADB are straight lines. ED is parallel to CB. Angle $CED = 122^{\circ}$ Angle $ABC = 59^{\circ}$

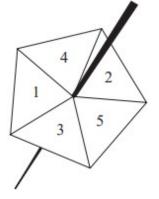
Work out the size of angle *CAB*. You must give a reason for each stage of your working.



(Total for Question 8 is 5 marks)

R

Roy spins a biased 5-sided spinner 48 times.



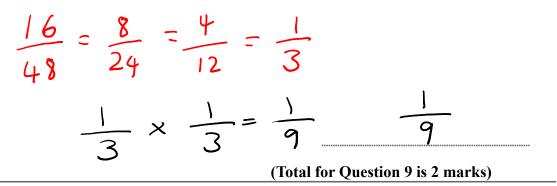
Here are his results.

9

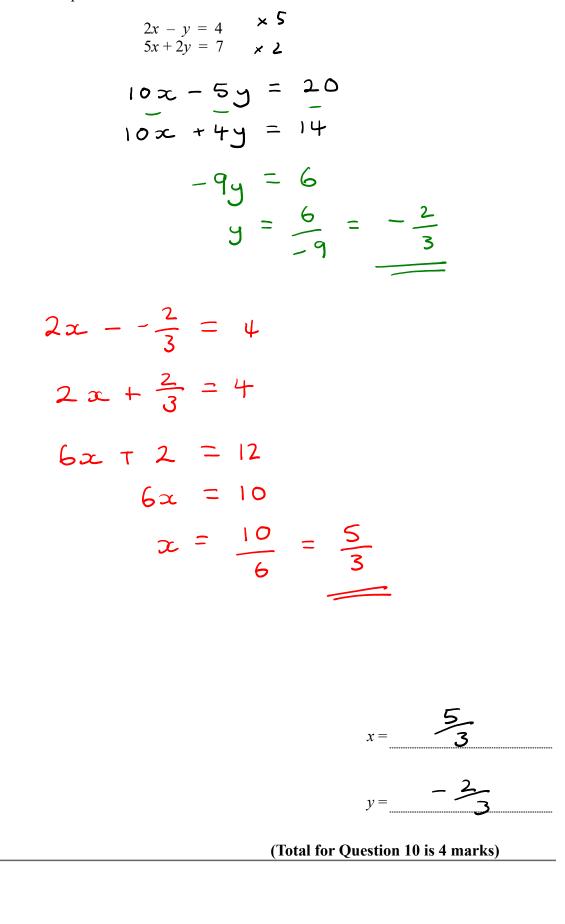
Score	1	2	3	4	5
Frequency	9	10	6	7	16

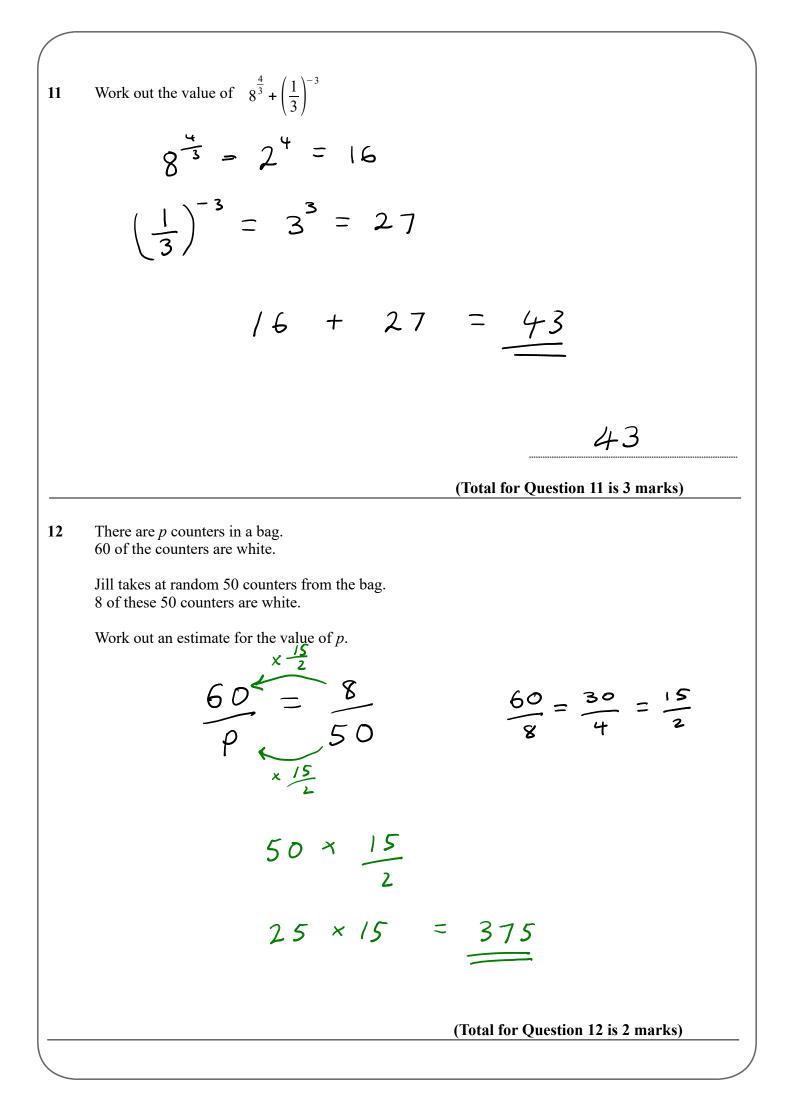
Roy is now going to spin the spinner another two times.

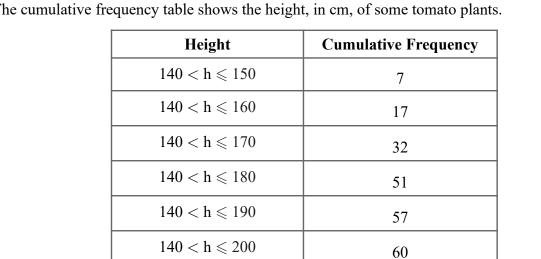
Work out an estimate for the probability that he gets a score of 5 both times



Solve the simultaneous equations

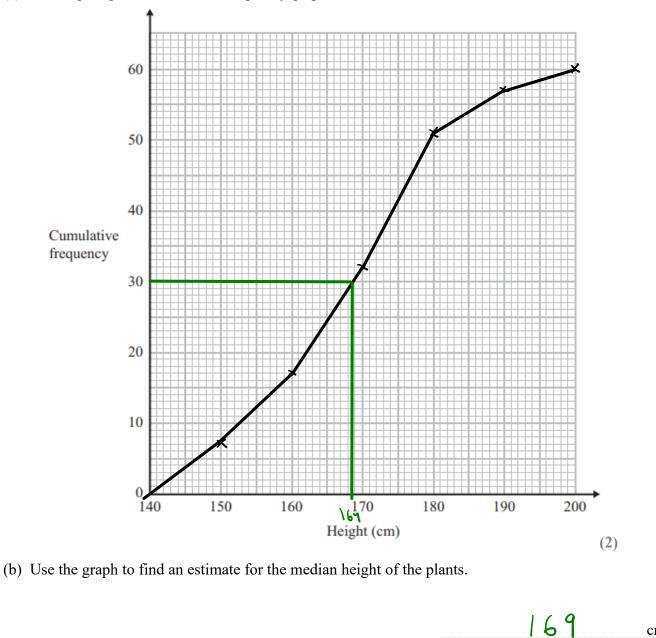






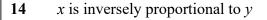
13 The cumulative frequency table shows the height, in cm, of some tomato plants.

(a) On the grid, plot a cumulative frequency graph for this information.

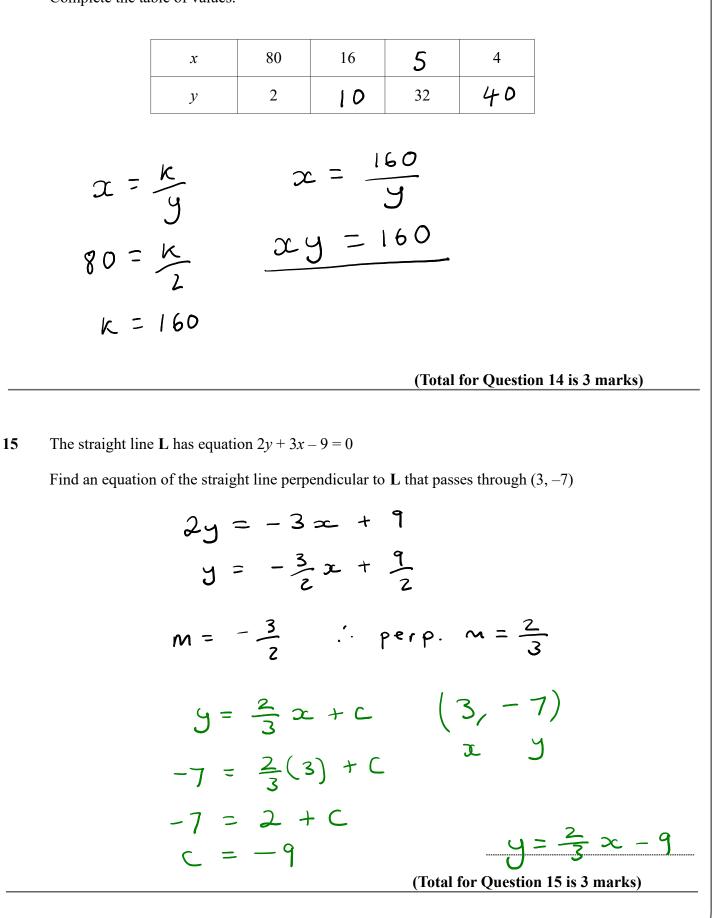


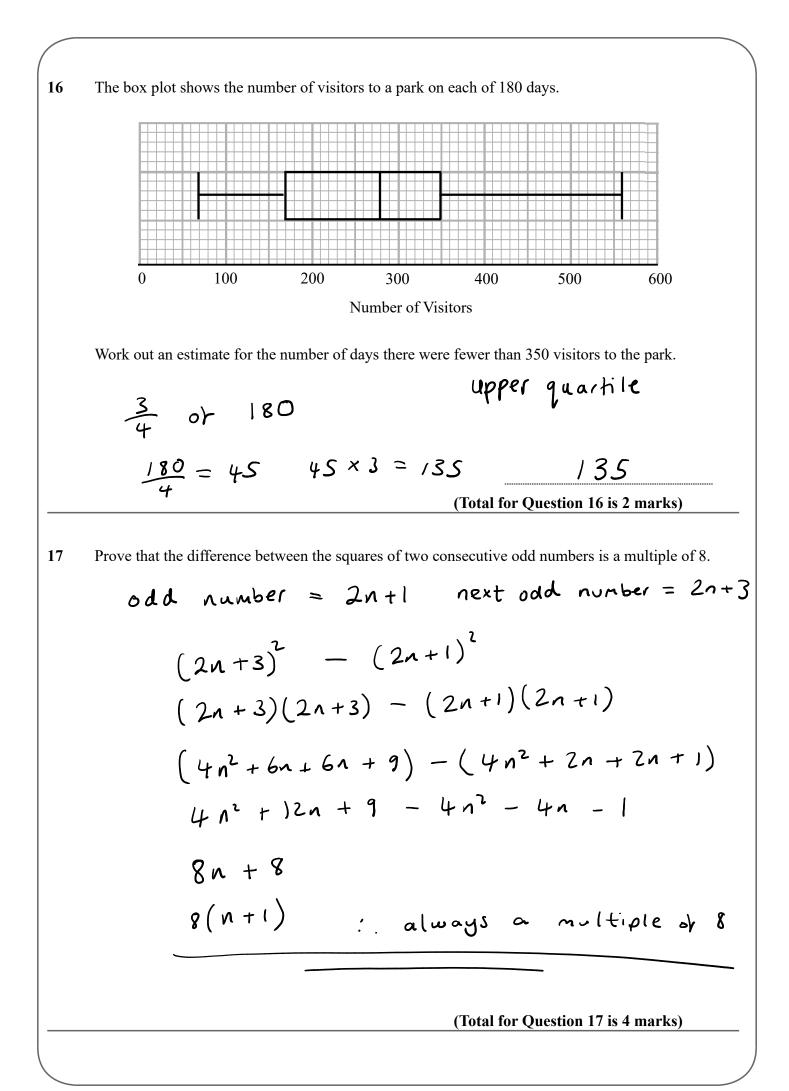
(1) (Total for Question 13 is 3 marks)

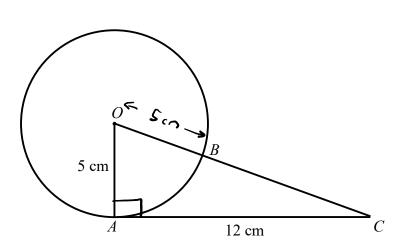
cm



Complete the table of values.







A and B is a point on the circumference of a circle, centre O. AC is a tangent to the circle. OBC is a straight line.

OA = 5 cmAC = 12 cm

Find the length of *BC*. You must show all your working.

$$OA^{2} + AC^{2} = OC^{2}$$

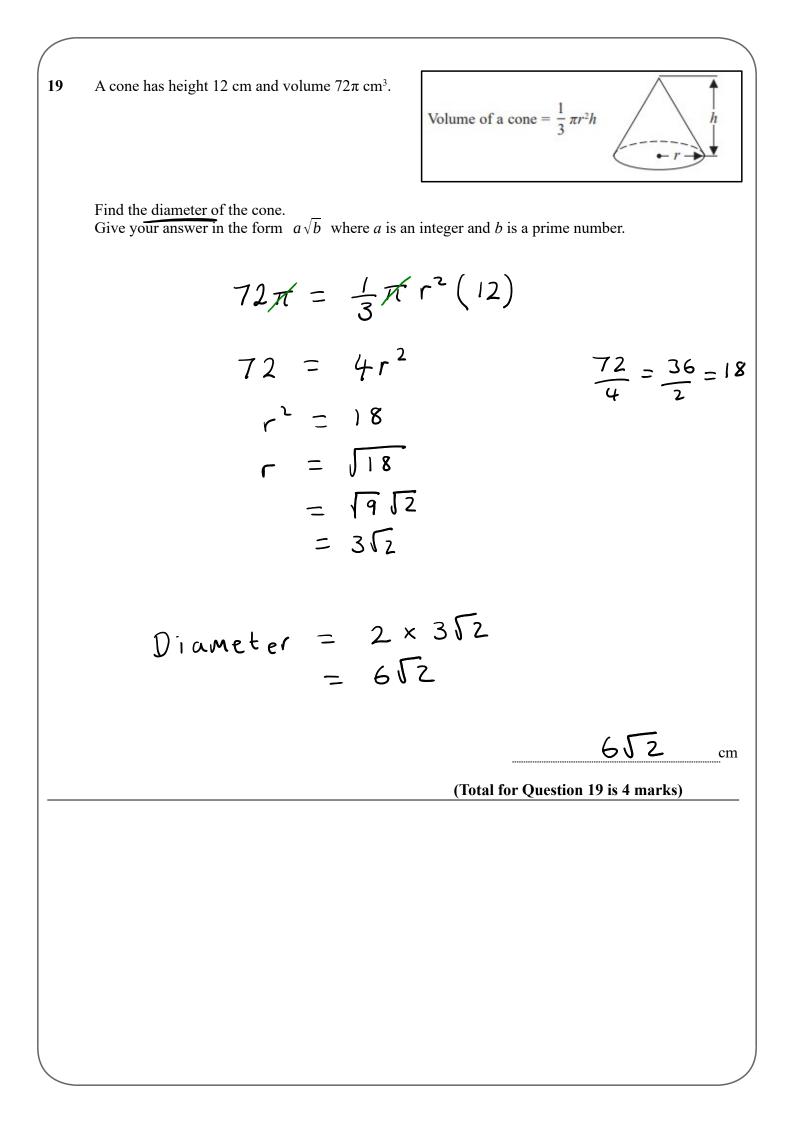
 $5^{2} + 12^{2} = OC^{2}$
 $169 = OC^{2}$
 $OC = 13 cm$

OB is a radius : 5cm

$$BC = 13 - 5$$
$$= 8 cm$$

cm

(Total for Question 18 is 4 marks)



20 *A*, *B* and *C* are three points such that

$$\overrightarrow{AB} = 6\mathbf{a} + 9\mathbf{b}$$
$$\overrightarrow{AC} = 10\mathbf{a} + 15\mathbf{b}$$

(a) Prove that *A*, *B* and *C* lie on a straight line.

$$\overrightarrow{AB} = 3(2a + 3b)$$

 $\overrightarrow{AC} = 5(2a + 3b)$
 \overrightarrow{AB} and \overrightarrow{AC} are both multiples of $2a + 3b$
and both pass through A. \therefore on a straight
line. (2)

$$\overrightarrow{DE} = 4\mathbf{a} - 5\mathbf{b}$$
$$\overrightarrow{EF} = -12\mathbf{a} + 15\mathbf{b}$$

Find the ratio

length of *DF* : length of *DE*

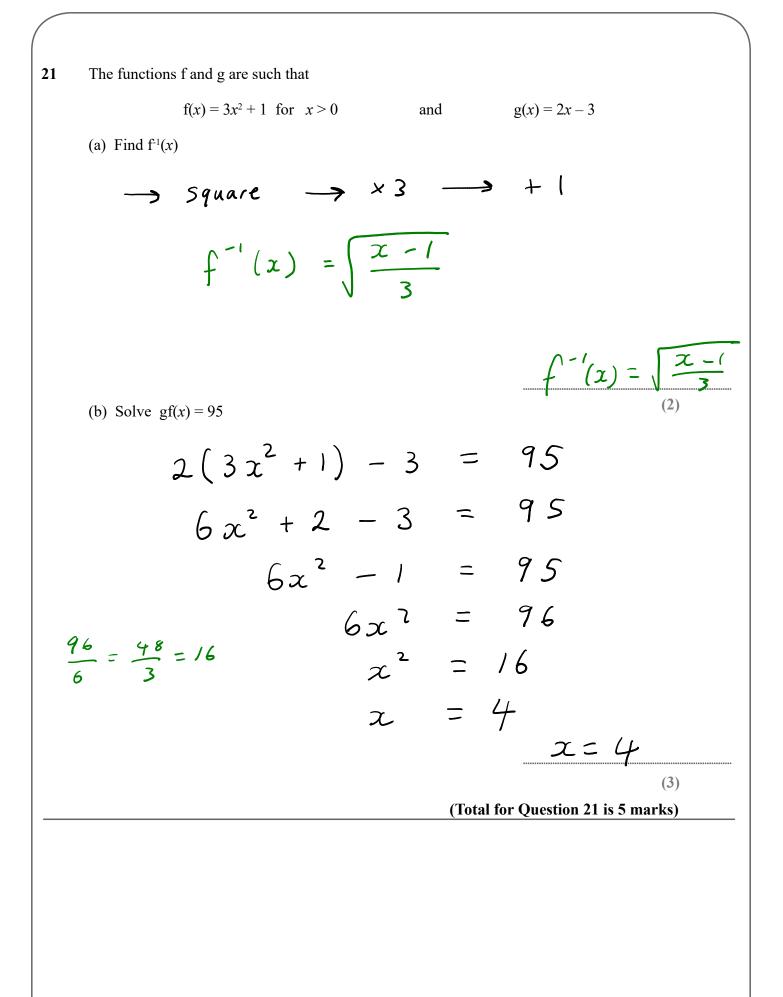
$$\overrightarrow{DF} = \overrightarrow{DE} + \overrightarrow{EF}$$

$$= \begin{pmatrix} 4 \\ -5 \end{pmatrix} + \begin{pmatrix} -12 \\ 15 \end{pmatrix} = \begin{pmatrix} -8 \\ 10 \end{pmatrix}$$

$$= -8a + 10b$$

$$\overrightarrow{DE} = \begin{pmatrix} 4 \\ -5 \end{pmatrix} \qquad \overrightarrow{DF} = \begin{pmatrix} -8 \\ 10 \end{pmatrix}$$

$$\overrightarrow{DF} \text{ is twice as long} \qquad 2:1$$
(3)
(Total for Question 20 is 5 marks)



Find the set of values of *x* for which

$$25 - x^2 > 0$$
 and $3x^2 - 17x - 6 < 0$

You must show all your working.

