

Write your name here

Surname

Other Names

# Mathematics

## 2018 Practice Paper Paper 1 (Non-Calculator) Higher Tier

Time: 1 hour 30 minutes

**You must have:** Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser.

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Answer the questions in the spaces provided – there may be more space than you need.
- **Calculators may not be used.**
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must **show all your working out.**



### Information

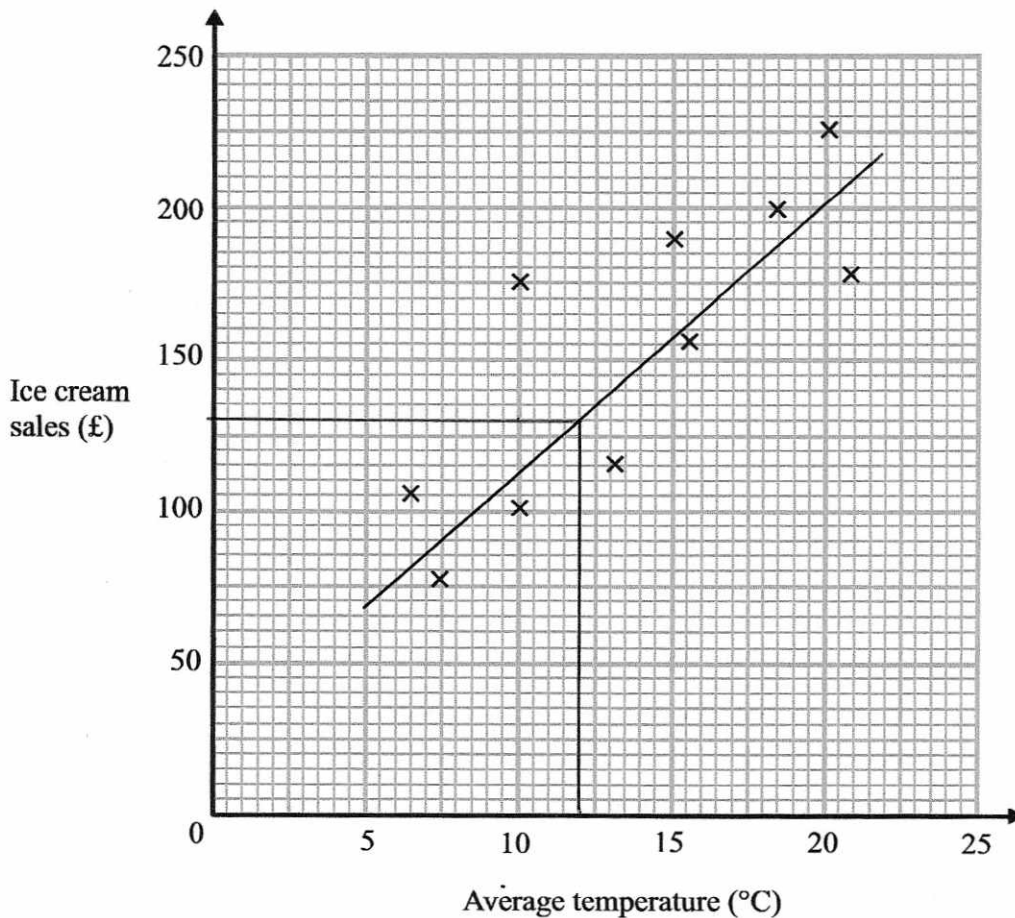
- The total mark for this paper is 80
- The marks for **each** question are shown in brackets – use this as a guide as to how much time to spend on each question.

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

- 1 The average daytime temperature for 10 days is recorded.  
A shop also records its ice cream sales for each of the 10 days.

The scatter graph shows this information.



- (a) What type of correlation does the scatter graph show?

..... positive ..... (1)

- (b) On the 11<sup>th</sup> day the temperature was 12°. Estimate the ice cream sales on the 11th day.

..... £130 .....  
..... £125 - £145 ..... (2)

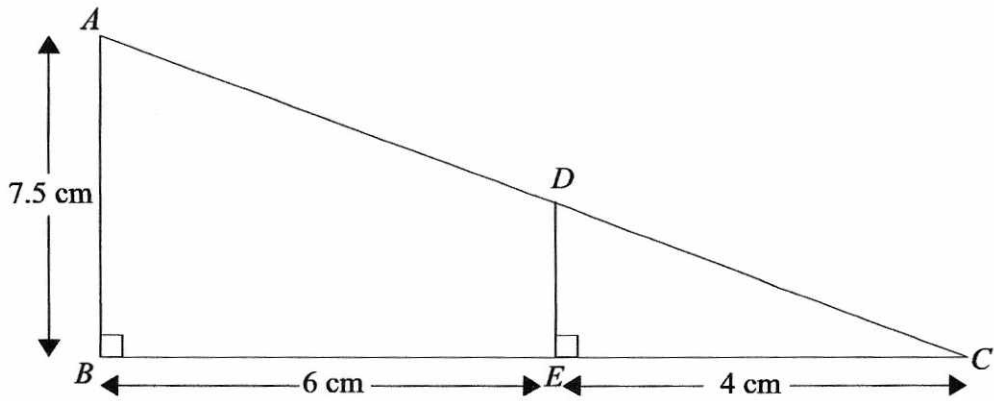
- (c) The shop's manager wants to use the scatter graph to predict the ice cream sales for a day with an average temperature of 2°C. Comment on the reliability of this prediction.

..... It is not reliable 2°C is not within the range of data we have .....  
.....

(1)

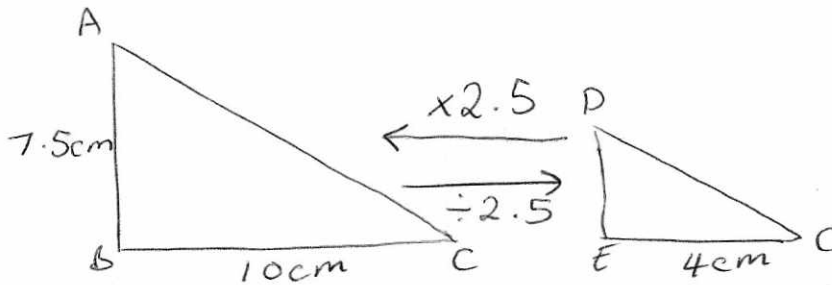
(Total for question 1 is 5 marks)

2



Scale factor =  $\frac{10}{4} = 2.5$

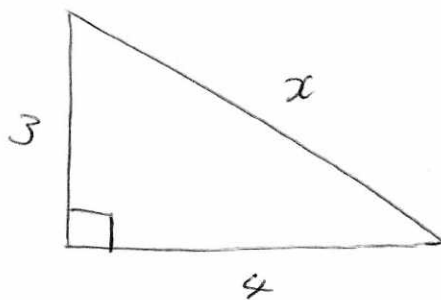
(a) Find the length of DE



$7.5 \div 2.5$

.....3.....cm  
(1)

(b) Find the length of DC



$3^2 + 4^2 = x^2$

$9 + 16 = x^2$

$25 = x^2$

$x = 5$

.....5.....cm  
(2)

(Total for question 2 is 3 marks)

3 Stevie has some marbles.

Freddie has twice as many marbles as Stevie.  $x$   $2x$

Danny has 5 more marbles than Freddie.

In total they have 55 marbles.  $2x + 5$

How many marbles does Danny have?

$$x + 2x + 2x + 5 = 55$$

$$5x + 5 = 55$$

$$5x = 50$$

$$x = 10$$

$$\text{Danny has: } 2(10) + 5 = \underline{\underline{25}}$$

.....  
25

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(Total for question 3 is 3 marks)

- 4 Rachel drives 300 miles from London to Newcastle.  
She drives the first 165 miles at an average speed of 60 mph.  
From this point it takes Rachel 3 hours and 15 minutes to complete her journey.



What was Rachel's average speed for the whole journey?

$$\text{Av speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

$$\begin{aligned} \text{First part of journey: time} &= \frac{\text{distance}}{\text{speed}} \\ &= \frac{165}{60} = \frac{33}{12} = \frac{11}{4} \\ &= 2\frac{3}{4} \text{ hours} \end{aligned}$$

$$\begin{aligned} \text{Total time} &= 3 \text{ hr } 15 + 2 \text{ hr } 45 \\ &= 6 \text{ hours} \end{aligned}$$

$$\text{Av speed} = \frac{300}{6} = 50$$

.....50.....mph

(Total for question 4 is 4 marks)

- 5 In a sale, normal prices are reduced by 25%.  
Freddie bought a car in the sale.  
The sale price of the car was £7500.  
Work out the normal price of the car.

$$£ 7500 = 75\%$$

$$£ 2500 = 25\%$$

$$£ 10000 = 100\%$$

£.....10000.....

(Total for question 5 is 2 marks)

- 6 The distance from Earth to Mars is approximately  $7.834 \times 10^{10}$  m.  
The distance from Earth to Neptune is approximately  $4.3514 \times 10^{12}$  m.

(a) Estimate how many times further away Neptune is from Earth than Mars is from Earth.

$$\frac{8 \times 10^{10}}{4 \times 10} \quad \frac{4 \times 10^{12}}{8 \times 10^{10}} = 0.5 \times 10^2$$

$$= \underline{\underline{50}}$$

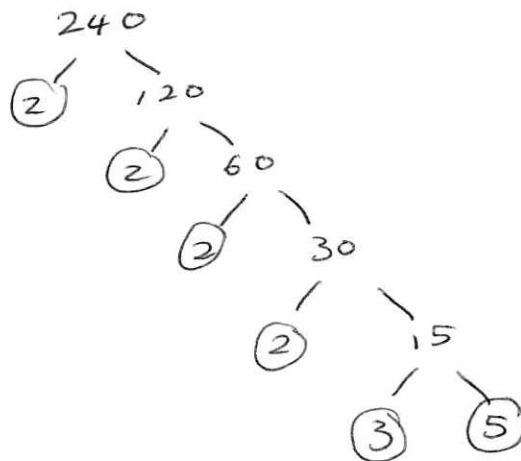
$$\frac{50}{(3)}$$

(b) Is your answer to part (a) an underestimate or an overestimate?  
Give a reason for your answer.

underestimate. I rounded the numerator down and the denominator up  $\rightarrow$  the actual answer would be bigger. (1)

(Total for question 6 is 4 marks)

- 7 Write 240 as a product of its prime factors.



$$2^4 \times 3 \times 5 \quad \text{or} \quad 2 \times 2 \times 2 \times 2 \times 3 \times 5$$

$$\underline{\underline{2 \times 2 \times 2 \times 2 \times 3 \times 5}}$$

(Total for question 7 is 3 marks)

8 Two maths classes, class A and class B, took a test.

The mean score of the 18 students in class A was 50%.

The mean score of the 22 students in class B was 70%.

What was the mean score of all 40 students?

$$\begin{aligned} \text{Total score class A} &= 18 \times 50 \\ &= 900 \end{aligned}$$

$$\text{Total score class B} = 22 \times 70$$

$$\begin{array}{r} 20 \times 70 = 1400 \\ 2 \times 70 = 140 \\ \hline 22 \times 70 = 1540 \end{array}$$

$$\begin{aligned} \text{Total score (all)} &= 900 + 1540 \\ &= 2440 \end{aligned}$$

$$\text{Mean} = \frac{2440}{40} = \frac{244}{4} = \frac{122}{2} = 61$$

.....61.....%

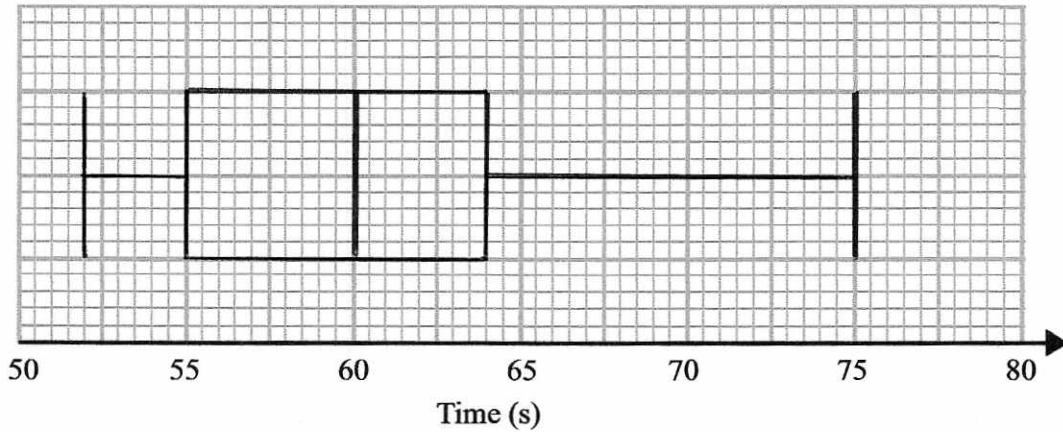
**(Total for question 8 is 3 marks)**

9 The times of 15 students running a race are recorded below.

52 54 54 55 58 58 59 60 61 61 64 67 70 75

Draw a box plot for this information.

Median = 60 L.Q. = 55 U.Q. = 64



(Total for question 9 is 2 marks)

10 In a cinema the ratio of adults to children is 3:1  $\frac{1}{4}$  children  
 The ratio of boys to girls is 3:2  $\frac{2}{5}$  girls  
 What fraction of all the people in the cinema are girls?

$$\frac{1}{4} \times \frac{2}{5} = \frac{2}{20} = \frac{1}{10}$$

$\frac{1}{10}$

(Total for question 10 is 3 marks)



11 Expand and Simplify  $(x+5)(x-3)(2x-1)$

$$(x^2 - 3x + 5x - 15)(2x - 1)$$

$$(x^2 + 2x - 15)(2x - 1)$$

$$2x^3 - x^2 + 4x^2 - 2x - 30x + 15$$

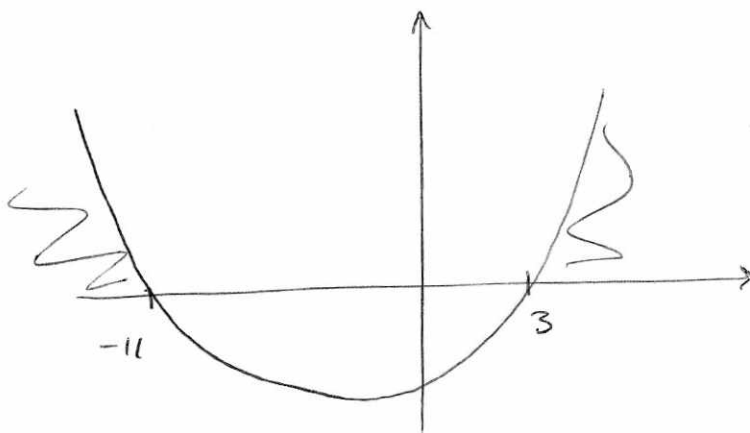
$$\underline{2x^3 + 3x^2 - 32x + 15}$$

(Total for question 11 is 3 marks)

12 Solve the inequality  $x^2 + 8x - 33 > 0$

$$(x + 11)(x - 3) > 0$$

$$x = -11 \quad x = 3$$



$$\underline{x < -11 \text{ or } x > 3}$$

(Total for question 12 is 4 marks)

13 Prove algebraically that the recurring decimal  $0.\dot{6}\dot{8}\dot{1}$  can be written as  $\frac{15}{22}$

$$\begin{aligned}0.\dot{6}\dot{8}\dot{1} &= x \\6.\dot{8}\dot{1} &= 10x \\681.\dot{8}\dot{1} &= 1000x \\675 &= 990x\end{aligned}$$

$$x = \frac{675}{990} = \frac{67.5}{99} = \frac{135}{198} = \frac{45}{66} = \frac{15}{22}$$

(Total for question 13 is 2 marks)

14 Make  $x$  the subject of the formula  $2x + a = b(x - 2)$

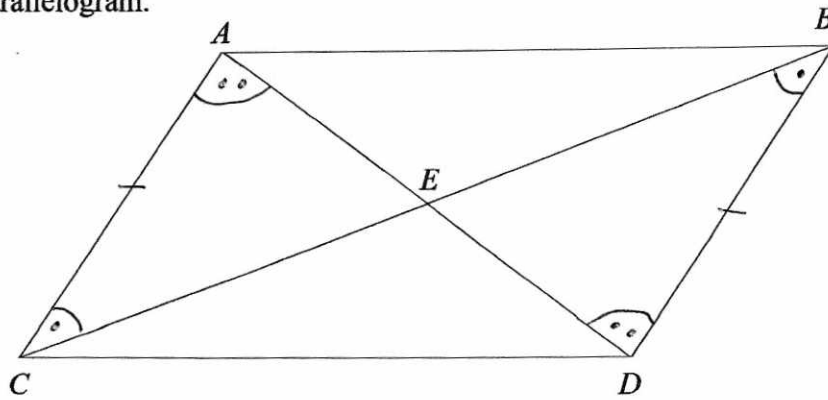
$$\begin{aligned}2x + a &= bx - 2b \\2x - bx &= -2b - a \\x(2 - b) &= -2b - a \\x &= \frac{-2b - a}{2 - b}\end{aligned}$$

$$\cancel{0x} x = \frac{2b + a}{b - 2}$$

$$x = \frac{-2b - a}{2 - b}$$

(Total for question 14 is 3 marks)

15  $ABCD$  is a parallelogram.



$E$  is the point where the diagonals  $AD$  and  $BC$  meet.  
Prove that triangle  $ACE$  and triangle  $BDE$  are congruent.

$AC = BD$  opposite sides in a parallelogram

$\angle ACE = \angle EBD$  alternate angles are equal

$\angle CAE = \angle EDB$  alternate angles are equal

$\triangle ACE$  and  $\triangle BDE$  are congruent ASA

(Total for question 15 is 4 marks)

16 Prove that the sum of the squares of two consecutive odd numbers is always 2 more than a multiple of 8

$$(2n+1)^2 + (2n+3)^2$$

$$(2n+1)(2n+1) + (2n+3)(2n+3)$$

$$4n^2 + 2n + 2n + 1 + 4n^2 + 6n + 6n + 9$$

$$8n^2 + 16n + 10$$

$$8n^2 + 16n + 8 + 2$$

$$\underbrace{8(n^2 + 2n + 1)}_{\text{Multiple of 8}} + \underbrace{2}_{+2}$$

(Total for question 16 is 2 marks)

17 Find the value of  $\left(\frac{64}{125}\right)^{-\frac{2}{3}} = \left(\frac{4}{5}\right)^{-2} = \left(\frac{5}{4}\right)^2 = \frac{25}{16}$

$$\frac{25}{16}$$

(Total for question 17 is 2 marks)

18  $c$  is inversely proportional to  $d$

When  $c = 15$ ,  $d = 4$

Find the value of  $c$  when  $d = 12$

$$c = \frac{k}{d}$$

$$15 = \frac{k}{4}$$

$$\underline{\underline{60 = k}}$$

$$c = \frac{60}{d}$$

$$c = \frac{60}{12}$$

$$= 5$$

$$c = \dots\dots\dots 5 \dots\dots\dots$$

(Total for question 18 is 3 marks)

19 Simplify fully  $\frac{(4 + 2\sqrt{3})(4 - 2\sqrt{3})}{\sqrt{11}}$

$$2\sqrt{3} \times 2\sqrt{3} = 4\sqrt{9} = 4 \times 3 = 12$$

You must show all your working.

$$\frac{16 - 8\sqrt{3} + 8\sqrt{3} - 12}{\sqrt{11}}$$

$$\frac{4 \times \sqrt{11}}{\sqrt{11} \times \sqrt{11}} = \frac{4\sqrt{11}}{\underline{\underline{11}}}$$

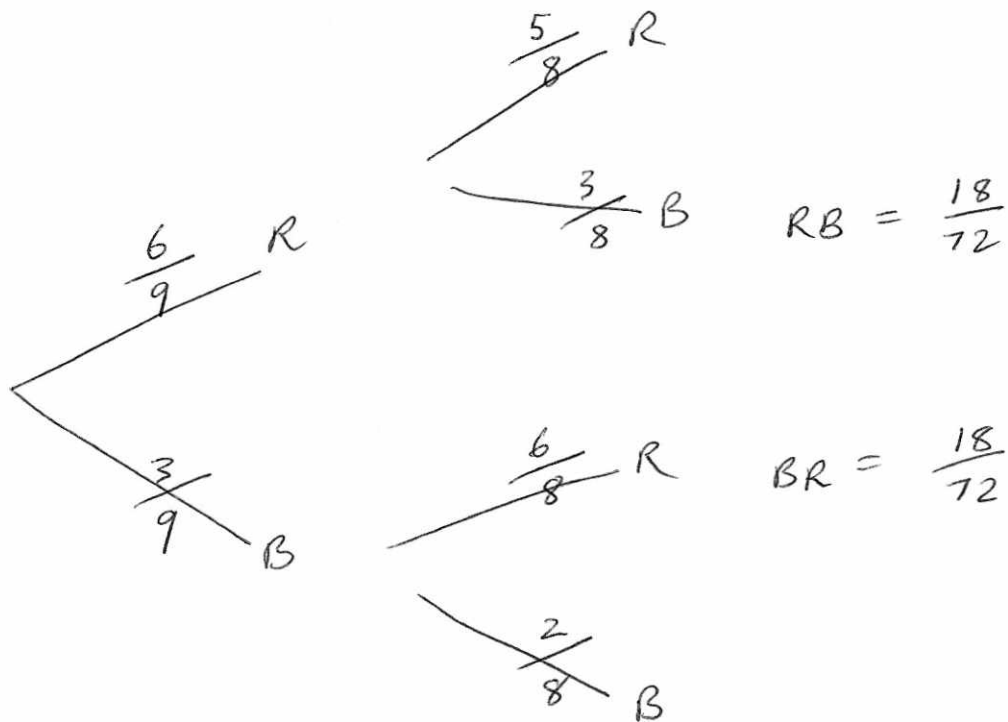
(Total for question 19 is 3 marks)

20 There are 6 red counters and 3 blue counters in a bag.

Joe takes at random a counter from the bag and does not replace it.

He then takes at random a second counter from the bag.

Calculate the probability that Joe has one counter of each colour.



$$\frac{18}{72} + \frac{18}{72} = \frac{36}{72} \quad \text{OR} \quad \frac{1}{2}$$

$$\frac{1}{2}$$

(Total for question 20 is 3 marks)

21 Solve the simultaneous equations

$$x^2 + y^2 = 26$$

$$2x - y = 3 \quad 2x = 3 + y$$

$$y = 2x - 3$$

$$x^2 + (2x - 3)^2 = 26$$

$$x^2 + (2x - 3)(2x - 3) = 26$$

$$x^2 + 4x^2 - 6x - 6x + 9 = 26$$

$$5x^2 - 12x + 9 = 26$$

$$5x^2 - 12x - 17 = 0$$

$$\frac{(5x + 5)(5x - 17)}{5} = 0$$

$$5 \times 17 = 85$$

$$\begin{array}{r} / \quad \backslash \\ 1 \quad 85 \\ 5 \quad 17 \end{array}$$

$$(x + 1)(5x - 17) = 0$$

$$x = -1 \quad x = \frac{17}{5}$$

$$y = 2(-1) - 3 = \underline{\underline{-5}}$$

$$y = 2\left(\frac{17}{5}\right) - 3$$

$$= \frac{34}{5} - 3$$

$$= \frac{34}{5} - \frac{15}{5}$$

$$= \underline{\underline{\frac{19}{5}}}$$

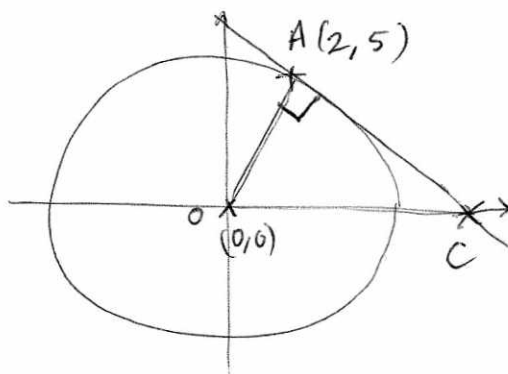
$$x = \dots -1 \text{ or } \frac{17}{5} \dots$$

$$y = \dots -5 \text{ or } \frac{19}{5} \dots$$

(Total for question 21 is 5 marks)

- 22 The line  $l$  is a tangent to the circle  $x^2 + y^2 = 29$  at the point  $A$ .  
 $A$  is the point  $(2, 5)$ .

The line  $l$  crosses the  $x$  axis at the point  $C$ .  
 Work out the area of triangle  $OAC$ .



gradient of  $OA$

$$= \frac{5-0}{2-0} = \frac{5}{2}$$

$AC$  is perpendicular to  $OA \therefore m = -\frac{2}{5}$

$$y = -\frac{2}{5}x + c \quad \begin{matrix} (2, 5) \\ x \quad y \end{matrix}$$

$$5 = -\frac{2}{5}(2) + c$$

$$5 = -\frac{4}{5} + c$$

$$\frac{25}{5} = \frac{-4}{5} + c$$

$$c = \frac{29}{5}$$

$$y = -\frac{2}{5}x + \frac{29}{5}$$

Crosses  $x$  axis when  
 $y = 0$

$$0 = -\frac{2}{5}x + \frac{29}{5}$$

$$\frac{2}{5}x = \frac{29}{5}$$

$$2x = 29$$

$$x = 14.5$$

Base 14.5  
 Height 5

Area of triangle =  $\frac{1}{2}$  base  $\times$  height

$$= \frac{1}{2} \times 14.5 \times 5$$

$$= \frac{1}{2} \times 72.5$$

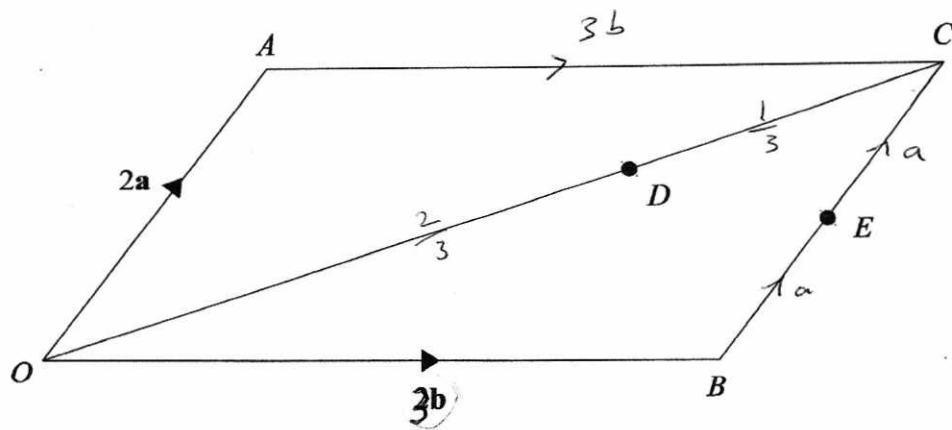
$$= \cancel{26.25}$$

$$36.25 = 36.25$$

$$\cancel{26.25} \quad (\text{units}^2)$$

(Total for question 22 is 5 marks)





$$\vec{OA} = 2a$$

$$\vec{OB} = 3b$$

D is the point on OC such that  $OD:DC = 2:1$

E is the midpoint of BC

Show that A, D and E are on the same straight line.

$$\vec{OC} = 2a + 3b$$

$$\vec{OD} = \frac{2}{3}(2a + 3b)$$

$$= \frac{4}{3}a + 2b$$

$$\vec{AD} = -2a + \frac{4}{3}a + 2b$$

$$= -\frac{2}{3}a + 2b$$

$$\vec{AE} = 3b - a$$

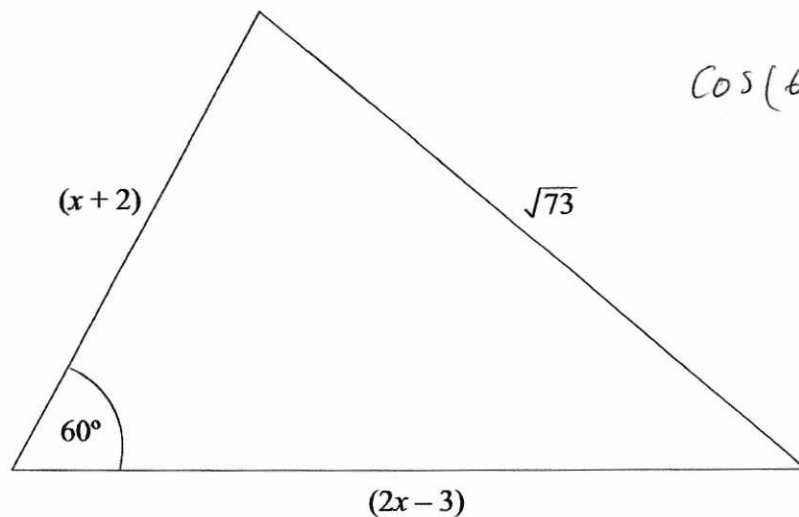
$$\vec{AD} = \frac{2}{3}(\cancel{3b} - a)$$

$$= \frac{2}{3}(3b - a)$$

A, D and E are on the same straight line.

$\vec{AE}$  and  $\vec{AD}$

They are parallel and pass through the same points.



$$\cos(60) = \frac{1}{2}$$

Work out the value of  $x$ .

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$73 = (x+2)^2 + (2x-3)^2 - 2(x+2)(2x-3) \cos(60)$$

$$73 = (x+2)(x+2) + (2x-3)(2x-3) - \cancel{2}(x+2)(2x-3) \left(\frac{1}{2}\right)$$

$$73 = x^2 + 2x + 2x + 4 + 4x^2 - 6x - 6x + 9 - (2x^2 - 3x + 4x - 6)$$

$$73 = 5x^2 - 8x + 13 - (2x^2 + x - 6)$$

$$73 = 5x^2 - 8x + 13 - 2x^2 - x + 6$$

$$73 = 3x^2 - 9x + 19$$

$$0 = 3x^2 - 9x - 54$$

$$0 = x^2 - 3x - 18$$

$$0 = (x - 6)(x + 3)$$

$$x = 6 \quad x = -3$$

$x$  cannot have a negative length.

$$\dots\dots\dots x = 6$$

(Total for question 24 is 5 marks)