

# Circles

$$\textit{Arc Length} = \frac{\theta}{2\pi} \times 2\pi r$$

$$\textit{Arc Length} = \theta r$$

$$\textit{Sector Area} = \frac{\theta}{2\pi} \times \pi r^2$$

$$\textit{Sector Area} = \frac{1}{2} \theta r^2$$

$$(x - a)^2 + (y - b)^2 = r^2$$

*Centre: (a, b)*

*Radius = r*

# Sequences and Series

$$U_n = ar^{(n-1)}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_\infty = \frac{a}{1-r}$$

*a = the first number*

*r = the common ratio*

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## The Binomial Expansion

Use Pascal's triangle or the  $nCr$  button

$$(a+b)^4$$

$$1a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + 1b^4$$

# Factors and Remainders

If  $(x+3)$  is a factor then  $f(-3)=0$

If  $f(-3)=5$  the remainder when you divide by  $(x+3)$  is 5.

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Divide  $x^3 + 4x^2 + 9x + 18$  by  $x + 3$

$$\begin{array}{r} x^2 + x + 6 \\ x+3 \overline{) x^3 + 4x^2 + 9x + 18} \\ \underline{x^3 + 3x^2} \phantom{+ 9x + 18} \\ x^2 + 9x \phantom{+ 18} \\ \underline{x^2 + 3x} \phantom{+ 18} \\ 6x + 18 \\ \underline{6x + 18} \\ 0 \end{array}$$

# Triangles

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## The Sine Rule

For Lengths:  $\frac{a}{\sin(A)} = \frac{b}{\sin(B)}$

For Angles:  $\frac{\sin(A)}{a} = \frac{\sin(B)}{b}$

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## The Cosine Rule

For Lengths:  $a^2 = b^2 + c^2 - 2bc \cos(A)$

For Angles:  $\cos(A) = \frac{b^2 + c^2 - a^2}{2bc}$

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$$Area = \frac{1}{2} ab \sin(C)$$

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And for right angled triangles:  
SOHCAHTOA and Pythagoras

# The Trapezium Rule

The gap between  
the x values is 2

$x$	2	4	6	8
$y$	3.2	3.7	3.9	4.0

Half the first and last, add them  
all up and multiply by the gap

$$2\left(\frac{3.2}{2} + 3.7 + 3.9 + \frac{4.0}{2}\right)$$

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# Differentiation

Turning Point

Stationary Point

Maximum

Minimum

All mean that  $\frac{dy}{dx} = 0$

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If  $\frac{d^2 y}{dx^2} > 0$  *minimum*

If  $\frac{d^2 y}{dx^2} < 0$  *maximum*

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# Integration

Area under curve between a and b =  $\int_a^b y dx$

# Logs

$$2^3 = 8$$

$$\log_2 8 = 3$$

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$$\log_a x + \log_a y = \log_a xy$$

$$\log_a x - \log_a y = \log_a (x/y)$$

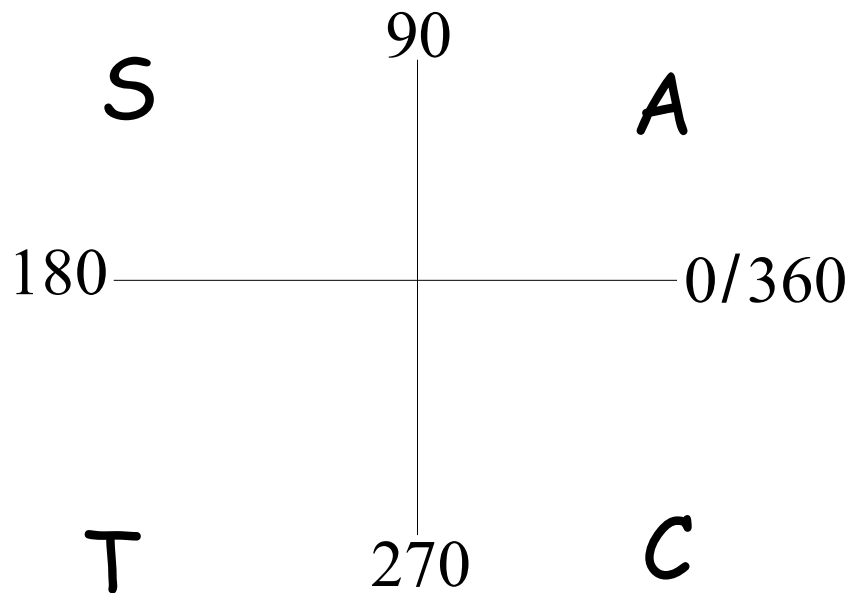
$$\log_a x^y = y \log_a (x)$$

# Trigonometry

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

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$$\sin(\theta) = \sin(180 - \theta)$$

$$\cos(\theta) = \sin(360 - \theta)$$

$$\tan(\theta) = \tan(\theta + 180)$$