1 Use the trapezium rule with n intervals of equal width to estimate the value of each integral.

a $\int_1^5 x \ln (x + 1)\ \mathrm{d}x$ $\quad n = 2$

b $\int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \cot x\ \mathrm{d}x$ $\quad n = 2$

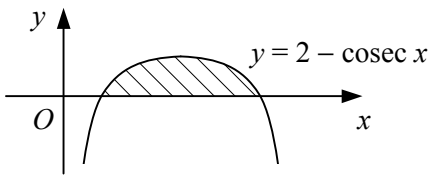
c $\int_{-2}^{2} \mathrm{e}^{\frac{x^2}{10}}\ \mathrm{d}x$ $\quad n = 4$

d $\int_0^1 \arccos (x^2 - 1)\ \mathrm{d}x$ $\quad n = 4$

e $\int_0^{0.5} \sec^2 (2x - 1)\ \mathrm{d}x$ $\quad n = 5$

f $\int_0^6 x^3\mathrm{e}^{-x}\ \mathrm{d}x$ $\quad n = 6$

2



The diagram shows the curve with equation $y = 2 - \operatorname{cosec} x,\ 0 < x < \pi$.

a Find the exact x-coordinates of the points where the curve crosses the x-axis.

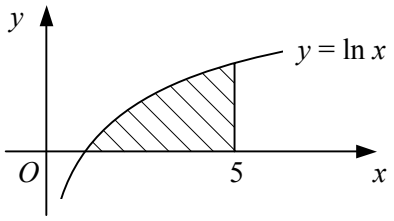
b Use the trapezium rule with four intervals of equal width to estimate the area of the shaded region bounded by the curve and the x-axis.

3 $\mathrm{f}(x) \equiv \frac{\pi}{6} + \arcsin (\frac{1}{2}x),\ x \in \mathbb{R}, -2 \leq x \leq 2.$

a Use the trapezium rule with three strips to estimate the value of the integral $I = \int_{-1}^{2} \mathrm{f}(x)\ \mathrm{d}x$.

b Use the trapezium rule with six strips to find an improved estimate for I.

4



The shaded region in the diagram is bounded by the curve $y = \ln x$, the x-axis and the line $x = 5$.

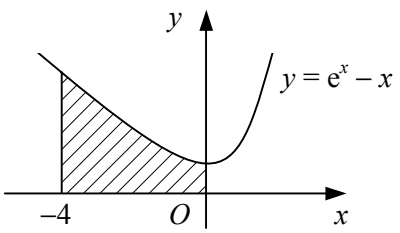
a Estimate the area of the shaded region to 3 decimal places using the trapezium rule with

i 2 strips **ii** 4 strips **iii** 8 strips

b By considering your answers to part **a**, suggest a more accurate value for the area of the shaded region correct to 3 decimal places.

c Use integration to find the true value of the area correct to 3 decimal places.

5



The shaded region in the diagram is bounded by the curve $y = \mathrm{e}^x - x$, the coordinate axes and the line $x = -4$. Use the trapezium rule with five equally-spaced ordinates to estimate the volume of the solid formed when the shaded region is rotated completely about the x-axis.