## Maths Genie Stage 14

# Test B

### Instructions

- Use **black** ink or ball-point pen.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.
- Calculators may be used.

### Information

- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.

### Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end





Solve  $36 - 9x \le x^2$ 2 (Total for Question 2 is 4 marks) The diagram shows two triangles, ABD and BCD.



Prove that triangle *ABD* is congruent to triangle *BCD*.

(Total for Question 3 is 3 marks)

3





(Total for Question 5 is 5 marks)



A, B and C are points on the circumference of a circle, centre O.

Prove that angle *AOC* is twice the size of angle *ABC*. You must **not** use any circle theorems in your proof.

(Total for Question 6 is 4 marks)

6





 $\overrightarrow{AB} = 3 a$  $\overrightarrow{DA} = a + b$  $\overrightarrow{DC} = 6 a$ 

E is the point where the line AC meets the line BD.

Find the ratio of the length of AE to the length of EC.

(Total for Question 7 is 5 marks)

8 There are 6 red counters and *y* blue counters in a bag.

Imogen takes a counter from the bag at random. Imogen then takes another counter at random from the bag.

The probability that the first counter Imogen takes is red and the second counter Imogen takes

is red is  $\frac{1}{8}$ 

Work how many blue counters are in the bag.

(Total for Question 8 is 5 marks)

9

- A circle has the equation  $x^2 + y^2 = 13$
- (a) Write down the exact length of the radius of the circle.

*P* is the point (-3,2) on the circle  $x^2 + y^2 = 13$ 

(b) Work out the equation of the tangent to the circle at P.

(4) (Total for Question 9 is 5 marks)

(1)