Name:

## Maths Genie Stage 13

## Test A

## Instructions

- Use black ink or ball-point pen.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.
- Calculators may be used.


## Information

- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end

1 (a) Write $x^{2}-8 x+3$ in the form $(x+a)^{2}+b$ where $a$ and $b$ are integers.
$\qquad$
(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y=x^{2}-8 x+3$
$\qquad$
$2 n$ is an integer.
Prove algebraically that the sum of $(n+3)(n+2)$ and $n+3$ is always a square number.

3 Sketch the graph of $y=\cos x^{\circ}$ for $0 \leq x \leq 360$


4 Write $\frac{x^{2}-x-30}{3 x^{2}+13 x-10}$ in the form $\frac{x+a}{b x+c}$ where $a, b$, and $c$ are integers.

5 There are 14 counters in a bag.
6 of the counters are red.
5 of the counters are blue.
3 of the counters are green.
Billie takes two counters are taken at random from the bag.
Work out the probability that the counters Billie takes are different colours.
You must show your working.

6 The diagram shows a cuboid $A B C D E F G H$.
$A B=6 \mathrm{~cm}$
$A E=5 \mathrm{~cm}$
$A G=15 \mathrm{~cm}$


Calculate the length of $A D$.
Give your answer correct to 3 significant figures.

7 The table shows information about the weight of 100 pigs.

| Weight (kg) | Frequency |
| :---: | :---: |
| $60<\mathrm{w} \leqslant 75$ | 12 |
| $75<\mathrm{w} \leqslant 85$ | 33 |
| $85<\mathrm{w} \leqslant 90$ | 25 |
| $90<\mathrm{w} \leqslant 110$ | 30 |

(a) On the grid, draw a histogram for the information in the table.

(b) Find an estimate for the median.
$\qquad$
.kg


The area of the triangle is $100 \mathrm{~m}^{2}$
Calculate the perimeter of triangle $A B C$.
Give your answer to 3 significant figures.
$9 \quad P=\frac{E}{t}$
$E=926$ correct to 3 significant figures
$t=8.5$ correct to 1 decimal place
By considering bounds, work out the value of $P$ to a suitable degree of accuracy.
Give a reason for your answer.

