## Mathematics

## Practice Set A

Paper 2 (Calculator)
Higher Tier

## Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres,
Total Marks protractor, pair of compasses, pen, HB pencil, eraser.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- Diagrams are NOT accurately drawn, unless otherwise indicated.

- You must show all your working out.


## Information

- The total mark for this paper is 80
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.

1 (a) Simplify $7 p^{6} \times 2 p^{-2}$
(b) Simplify $\left(3 x^{5} y^{2}\right)^{4}$
(c) $p^{2} \times p^{5}=p^{11} \times p^{y}$

Find the value of $y$

2 (a) Find the highest common factor (HCF) of 70 and 56
(b) Find the lowest common multiple (LCM) of 70 and 56


Find the equation of line $\mathbf{L}$.

4 Abbie buys a sofa for $£ 680$
She pays a deposit of $15 \%$ and the rest of the money in monthly payments of $£ 17$.
How many monthly payments will Abbie need to pay?

5 There are only green pens, black pens and red pens in a box.
There are five times as many green pens as black pens.
There are half as many red pens as green pens.
Write down the ratio of green pens to black pens to red pens.

6 (a) Complete the table of values for $y=x^{2}-x-2$

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |


(b) On the grid draw the graph of $y=x^{2}-x-2$ for values of $x$ from -2 to 4
(c) Use the graph to find an estimate of the turning point of the graph $y=x^{2}-x-2$

7 In 2000, the world population was 6.1 billion.
In 2020, the world population was 7.8 billion.
Work out the percentage increase in population.
Give your answer correct to 1 decimal place.

8


The diagram shows a triangular prism.
The cross-section of the prism is a right angled triangle.
Calculate the volume of the prism.
$\mathrm{cm}^{3}$


On the grid, enlarge the triangle by scale factor -1.5 . centre $O$.
$10 \quad 100$ students in year 7 either study French or German or Spanish.
47 of the students are boys and the rest are girls.
12 boys study German.
15 boys and 16 girls study French.
A total of 32 students study Spanish.
Work out how many girls study Spanish.

11 Charlie invests $£ 2500$ for 3 years in a savings account.
She gets $3 \%$ per annum compound interest in the first year, then $x \%$ for 2 years.
Charlie has $£ 2705.36$ at the end of 3 years, work out the value of $x$.

12 Given that $\mathrm{f}(x)=x^{2}-7$ and $\mathrm{g}(x)=2 x+3$
(a) Work out an expression for $\mathrm{g}^{-1}(x)$
(b) Find $\mathrm{fg}(5)$

13 Here are four graphs.



D
$y$


Match each graph with a statement in the table below.

| Proportionality relationship | Graph letter |
| :--- | :--- |
| $y$ is directly proportional to $x$ |  |
| $y$ is inversely proportional to $x$ |  |
| $y$ is directly proportional to $x^{2}$ |  |
| $y$ is inversely proportional to $x^{2}$ |  |


$C, D$ and $E$ are points on a circle, centre $O$.
$A E B$ is a tangent to the circle at $E$.
$C D=D E$
Angle $A E C=x^{\circ}$
Find the size of angle $O E D$, in terms of $x$.
Give reasons for each stage of your working.

15 Here is a speed-time graph.

(a) Work out an estimate for the acceleration when $\mathrm{t}=4$.
$\qquad$
(b) Use 5 strips of equal width to find an estimate for the distance travelled in 10 seconds.

16 Each day Paul wears either a black tie or a red tie to work.
On Monday the probability he wears a black tie is 0.72
If Paul wears a black tie on Monday, the probability that he will wear a black tie on Tuesday is 0.24 If he does not wear a black tie on Monday, the probability that he will wear a black tie on Tuesday is 0.8
(a) Complete the probability tree diagram.

## Monday


(b) Work out the probability Paul wears different coloured ties on Monday and Tuesday .

17 (a) On the grid, draw the graph of $x^{2}+y^{2}=23.04$

(b) Hence find estimates for the solutions of the simultaneous equations

$$
\begin{aligned}
& x^{2}+y^{2}=23.04 \\
& x+2 y=4
\end{aligned}
$$

18 The table shows information about the speed, in mph, of 120 cars.

| Speed (mph) | Frequency |
| :---: | :---: |
| $40<\mathrm{s} \leqslant 55$ | 6 |
| $55<\mathrm{s} \leqslant 60$ | 15 |
| $60<\mathrm{s} \leqslant 65$ | 48 |
| $65<\mathrm{s} \leqslant 75$ | 44 |
| $75<\mathrm{s} \leqslant 90$ | 7 |

(a) On the grid, draw a histogram for the information in the table.

(b) Work out an estimate for the number of cars over 70 mph .

19 The diagram shows a triangular prism.
$C D=9 \mathrm{~cm}$
$A D=14 \mathrm{~cm}$
Angle $A D C=30^{\circ}$


Calculate the size of angle $A F C$.
Give your answer correct to 1 decimal place.

20 The diagram shows a solid shape.
The shape is a cone on top of a hemisphere.


The height of the cone is 12 cm .
The base of the cone has a diameter of 8 cm .
The diameter of the hemisphere is 8 cm .
Work out the total volume of the solid shape. Give your answer in terms of $\pi$.
$\mathrm{F}=20.1 \mathrm{~N}$ correct to 1 decimal places
$P=9.18 \mathrm{Nm}^{-2}$ correct to 3 significant figures

By considering bounds, work out the value of $A$ to a suitable degree of accuracy.
Give a reason for your answer.

$$
p=\frac{F}{A}
$$

$p=$ pressure
$F=$ force
$A=$ area
$\qquad$
.m ${ }^{2}$

