Name:

GCSE (1 - 9)

Repeated Percentage Change

Instructions

- Use black ink or ball-point pen.
- · Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- · Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.

Information

- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.

Advice

- · Read each question carefully before you start to answer it.
- · Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end

1 A population of bacteria is increasing by 10% each hour.

Find the percentage increase in the population every 3 hours.

$$1.1 \times 1.1 \times 1.1 = 1.331$$

$$(Ans -1) \times 100 = 33.1$$

33.1%

(Total for question 1 is 2 marks)

2 A shop decreases prices by 10% and then by a further 20%.

Rachel says: "Prices have now decreased by 30%".

Is Rachel correct?

You must show your working.

$$0.9 \times 0.8 = 0.72$$

(Total for question 2 is 2 marks)

3 Alex invests some money for 3 years in a savings account. She gets 4% per annum compound interest.

Alex has £5680.56 at the end of 3 years, work how much she invested.

$$3c \times 1.04^{3} = 5680.56$$

$$3c = \frac{5680.56}{1.04^{3}}$$

$$= \frac{1.04^{3}}{1.04^{3}}$$

£5050

(Total for question 3 is 3 marks)

4 Bailey invests some money for 5 years in a savings account. She gets 3% per annum compound interest.

Bailey has £3593.75 at the end of 5 years, work how much she invested.

$$x \times 1.03^5 = 3593.75$$

$$x = \frac{3593.75}{1.03^5}$$

$$= \frac{13100}{1.03}$$

£3100

(Total for question 4 is 3 marks)

5 Charlie invests £2500 for 3 years in a savings account.

She gets 3% per annum compound interest in the first year, then x% for 2 years.

Charlie has £2705.36 at the end of 3 years, work out the value of x.

$$2500 \times 1.03 \times y^{2} = 2705.36$$

$$y^{2} = \frac{2705.36}{2500 \times 1.03}$$

$$y^2 = 1.0506...$$

 $y = \sqrt{Ans}$
= 1.025

$$x = (Ams - 1) \times 100$$

= 2.5%

2.5%

(Total for question 5 is 4 marks)

6 Dana invests £5000 for 4 years in a savings account. She gets 2% per annum compound interest in the first year, then x% for 3 years.

Dana has £5508.23 at the end of 4 years, work out the value of x.

= 26%

$$5000 \times 1.02 \times y^{3} = 5508.23$$

$$y^{3} = 5508.23$$

$$5000 \times 1.02$$

$$= 1.080045$$

$$y = 1.026$$

$$DC = (Ans -1) \times 100$$

2.6%

(Total for question 6 is 4 marks)

7 A population model assumes that the number of people living in Stoverton is increasing by x% each year.

The population is expected to increase by 60% in 6 years, work out the value of x. Give your answer to 1 decimal place.

$$y' = 1.6$$
 $y = 1.6$
 $y = 1.0814$

$$x = (Ans - 1) \times 100$$

= 8.1%

8.1%

(Total for question 7 is 3 marks)

8 A car's value is decreasing by x% each year.

The car will half in value in 5 years, work out the value of x. Give your answer to 1 decimal place.

$$y^{5} = 0.5$$
 $y = 5\sqrt{0.5}$
 $y = 0.87055$

$$x = (1 - Ans) \times 100$$

$$= 12.9%$$

12.9%

(Total for question 8 is 3 marks)

9 The number of rabbits in a field is increasing by x% each year.

The population is expected to double in 5 years, work out the value of x. Give your answer to 1 decimal place.

$$y^{5} = 2$$
 $y = \sqrt{2}$
 $= 1.148698...$

14.9%.

(Total for question 9 is 3 marks)

10 A car's value is decreasing by x% each year.

The car's value will decrease by 60% in 6 years, work out the value of x. Give your answer to 2 decimal places.

$$y^{\circ} = 0.4$$
 $y = \sqrt{0.4}$
 $= 0.85837$

$$z = (1 - Ans) \times 100$$
= 14.16%

14.16%.

(Total for question 10 is 3 marks)

11 A circle's radius is increased by 8%. Find the increase in the circle's area.

$$A = \pi r^{2}$$

New circle: $A = \pi (1.08r)^{2}$
 $= 1.1664 \pi r^{2}$
 $(1.1664 - 1) \times 100 = 16.64\%$

(Total for question 11 is 4 marks)

12 A circle's area is increased by 5%. Find the increase in the circle's radius.

Give your answer to 1 decimal place.

$$A = \pi r^{2}$$

$$1.05A = \pi (xr)^{2}$$

$$1.05A = x^{2} \pi r^{2}$$

$$1.05 = x^{2}$$

$$x = 1.024695...$$

$$(Ans -1) \times 100 = 2.55$$

2.5%

(Total for question 12 is 4 marks)

13 A cube's length is increased by 12%. Find the increase in the cube's volume.

Give your answer to 3 significant figures.

New cube:
$$V = (1.121)^3$$

 $= 1.404928$ $= 1.404928$ $= 40.5\%$ (354)

(Total for question 13 is 4 marks)

14 A cube's volume is increased by 25%. Find the increase in the cube's length.

Give your answer to 3 significant figures.

$$1.25V = \left(\frac{\chi l}{1.25V} \right)^{3}$$

$$1.25V = \chi^{3} l^{3}$$

$$1.25 = \chi^{3}$$

$$\chi = 1.077217...$$

$$(Ams - 1) \times 100 = 7.72i. \quad (3sl)$$

7. 72%

(Total for question 14 is 4 marks)