

Name: \_\_\_\_\_

**IGCSE**  
**Circle Theorems**

**Instructions**

- Use **black** ink or ball-point pen.
- Answer all questions.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- You must **show all your working out.**

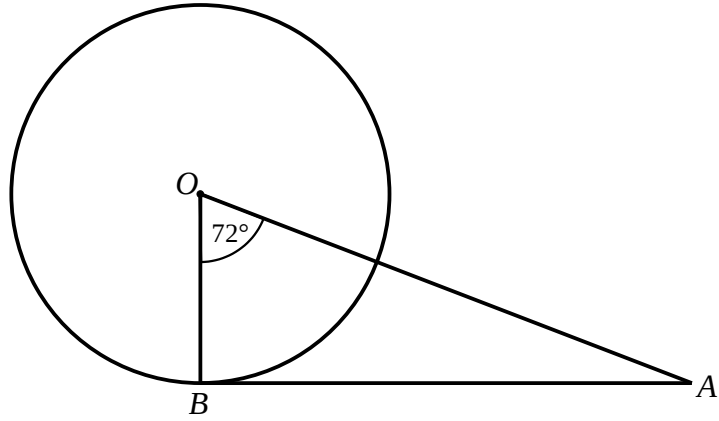
**Information**

- The marks for each question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

**Advice**

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end

1



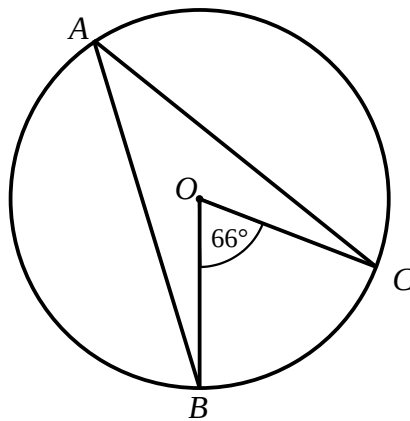
$B$  is a point on the circumference of a circle, centre  $O$ .  
 $AB$  is a tangent to the circle.

Angle  $BOA = 72^\circ$

Work out the size of angle  $BAO$ .  
You must show all your working.

.....  
(Total for Question 1 is 2 marks)

2



$A$ ,  $B$ ,  $C$  and  $D$  are points on the circumference of a circle.

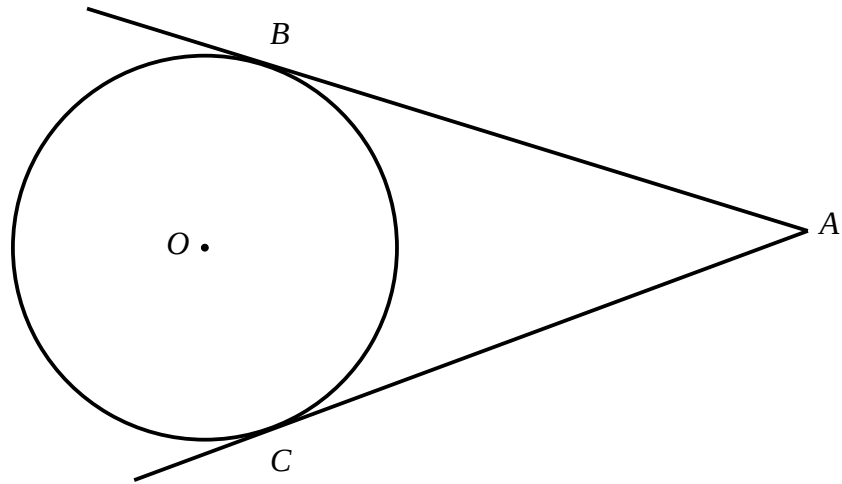
Angle  $BOC = 66^\circ$

(i) Find the size of angle  $BAC$ .

(ii) Give a reason for your answer.

.....  
.....  
.....  
(Total for Question 2 is 2 marks)

3



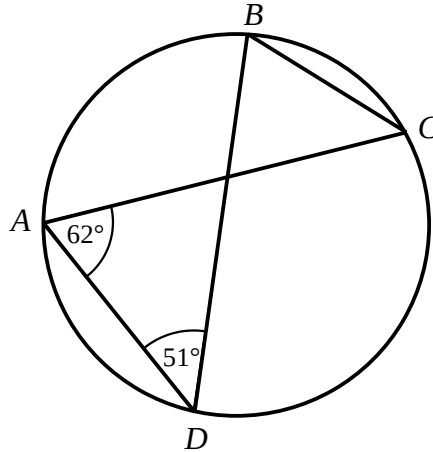
$B$  and  $C$  are points on a circle, centre  $O$ .  
 $AB$  and  $AC$  are tangents to the circle.

Angle  $BAC = 40^\circ$

Work out the size of angle  $BOC$ .  
You must show all your working.

.....  
(Total for Question 3 is 3 marks)

4



$A$ ,  $B$ ,  $C$  and  $D$  are points on the circumference of a circle.

Angle  $CAD = 62^\circ$

Angle  $ADB = 51^\circ$

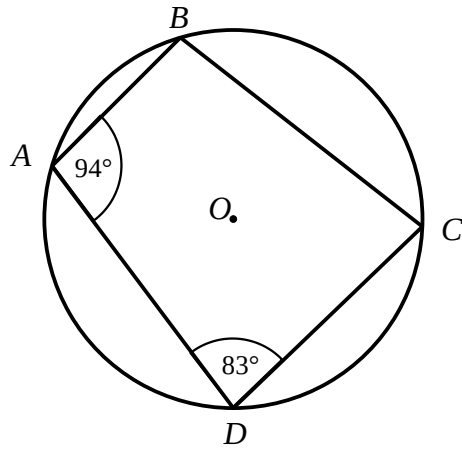
(i) Find the size of angle  $ACB$ .

(ii) Give a reason for your answer.

.....  
.....

(Total for Question 4 is 2 marks)

5



$A, B, C$  and  $D$  are points on the circumference of a circle.

Angle  $BAD = 94^\circ$

Angle  $ADC = 83^\circ$

(i) Find the size of angle  $ABC$ .

o

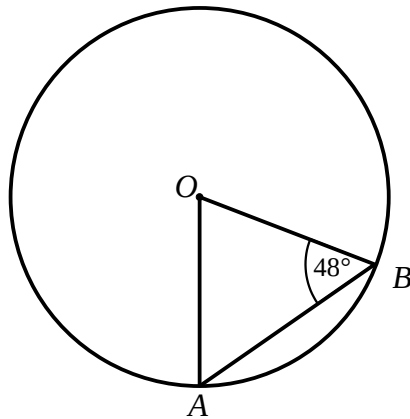
.....

(ii) Give a reason for your answer.

.....  
.....

**(Total for Question 5 is 2 marks)**

6



$A$  and  $B$  are points on the circumference of a circle, centre  $O$ .

Angle  $ABO = 48^\circ$

(i) Find the size of angle  $AOB$ .

o

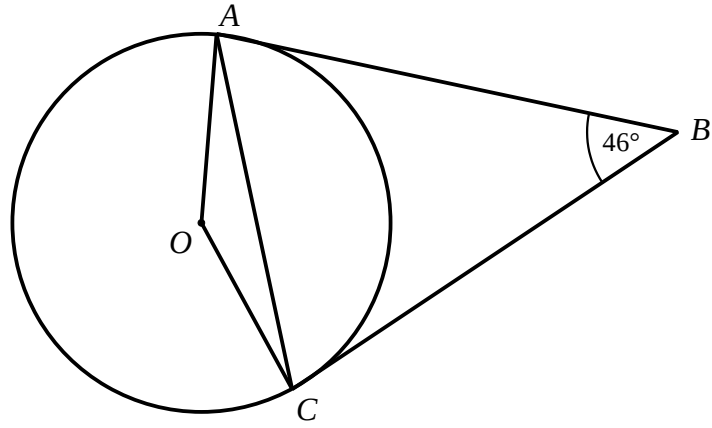
.....

(ii) Give a reason for your answer.

.....  
.....

**(Total for Question 6 is 2 marks)**

7



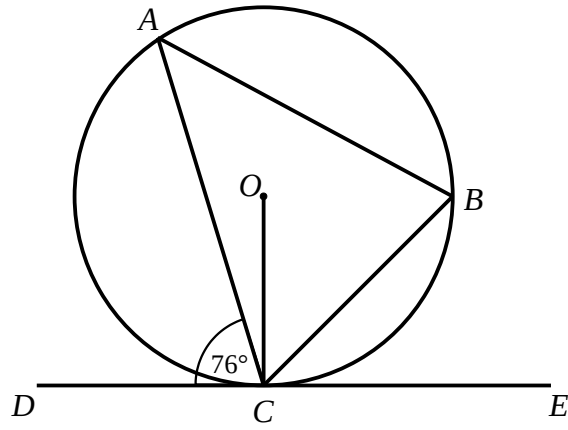
$A$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $AB$  and  $BC$  are tangents to the circle.

Angle  $ABC = 46^\circ$

Find the size of angle  $OAC$ .  
Give reasons for each stage of your working.

.....  
**(Total for Question 7 is 4 marks)**

8



$A$  and  $B$  are points on the circumference of a circle, centre  $O$ .  
 $DCE$  is a tangent to the circle.

Angle  $ACD = 76^\circ$

(a) Find the size of angle  $ACO$ .  
Give reasons for each stage of your working.

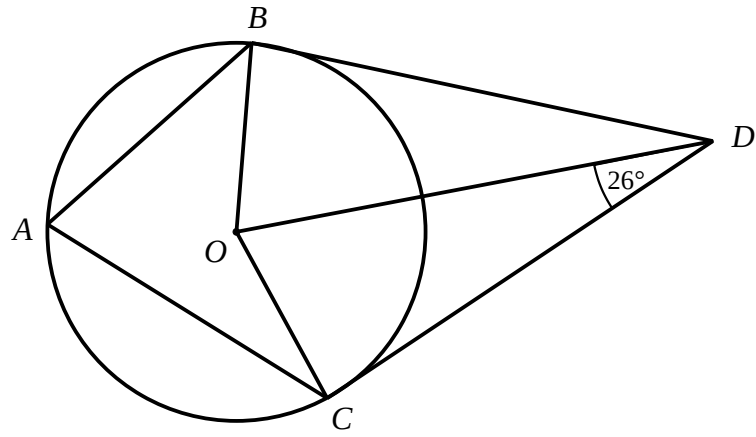
.....  
(2)

(b) Find the size of angle  $ABC$ .  
Give reasons for each stage of your working.

.....  
(2)

**(Total for Question 8 is 4 marks)**

9



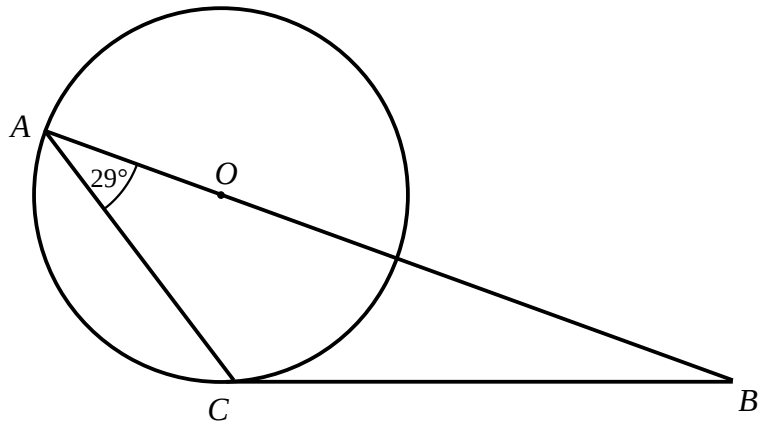
$A$ ,  $B$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $BD$  and  $CD$  are tangents to the circle.

Angle  $ODC = 26^\circ$

Find the size of angle  $BAC$ .  
Give reasons for each stage of your working.

.....  
(Total for Question 9 is 4 marks)

10



$A$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $BC$  is a tangent to the circle.

Angle  $CAB = 29^\circ$

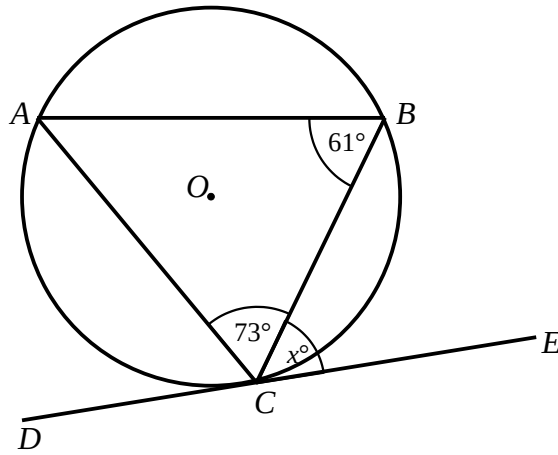
Find the size of angle  $ABC$ .  
You must show all your working.

o

.....  
(Total for Question 10 is 4 marks)



11



$A$ ,  $B$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $DCE$  is a tangent to the circle.

Angle  $ABC = 61^\circ$

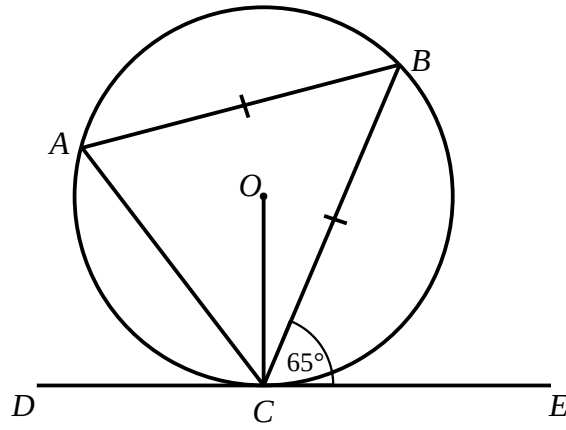
Angle  $ACB = 73^\circ$

Angle  $BCE = x^\circ$

Find the value of  $x$ .

Give reasons for each stage of your working.

.....  
**(Total for Question 11 is 3 marks)**



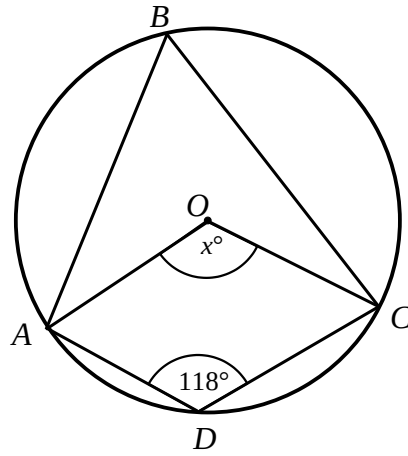
$A$ ,  $B$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $DCE$  is a tangent to the circle.

$AB = BC$   
 Angle  $BCE = 65^\circ$

Find the size of angle  $AOC$ .  
 You must show all your working.

.....  
 (Total for Question 12 is 4 marks)

13



$A$ ,  $B$ ,  $C$  and  $D$  are points on the circumference of a circle, centre  $O$ .

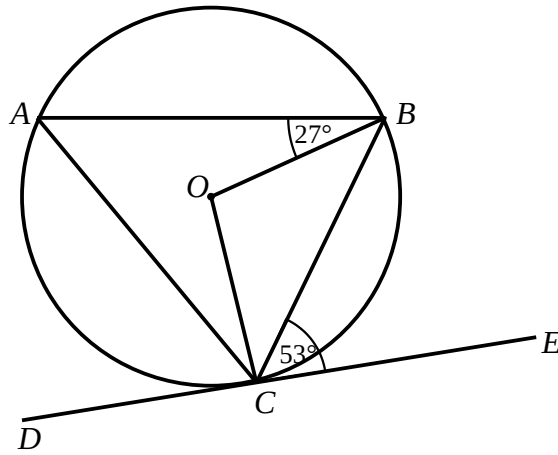
Angle  $ADC = 118^\circ$

Angle  $AOC = x^\circ$

Work out the value of  $x$ .

You must show all your working.

.....  
(Total for Question 13 is 3 marks)



$A$ ,  $B$  and  $C$  are points on the circumference of a circle, centre  $O$ .  
 $DCE$  is a tangent to the circle.

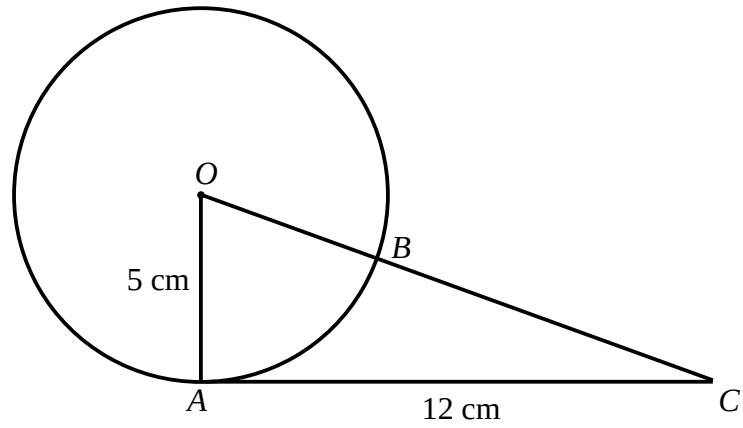
Angle  $ABO = 27^\circ$

Angle  $BCE = 53^\circ$

Find the size of angle  $ACO$ .

Give reasons for each stage of your working.

.....  
**(Total for Question 14 is 4 marks)**



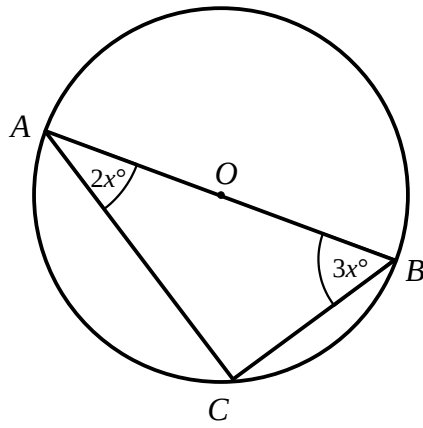
$A$  and  $B$  is a point on the circumference of a circle, centre  $O$ .  
 $AC$  is a tangent to the circle.  
 $OBC$  is a straight line.

$OA = 5$  cm  
 $AC = 12$  cm

Find the length of  $BC$ .  
You must show all your working.

..... cm

**(Total for Question 15 is 4 marks)**



$A$ ,  $B$  and  $C$  are points on the circumference of a circle, centre  $O$ .

$$\text{Angle } CAB = 2x^\circ$$

$$\text{Angle } ABC = 3x^\circ$$

Find the value of  $x$ .

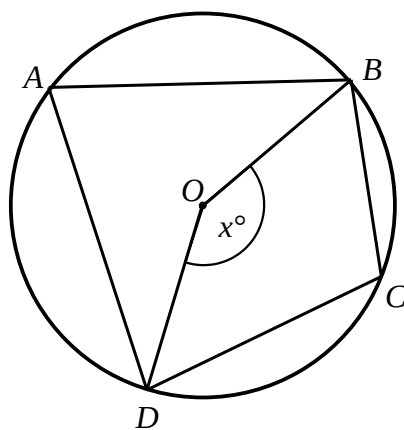
You must show all your working.

$$x = \dots\dots\dots$$

**(Total for Question 16 is 3 marks)**

---

17



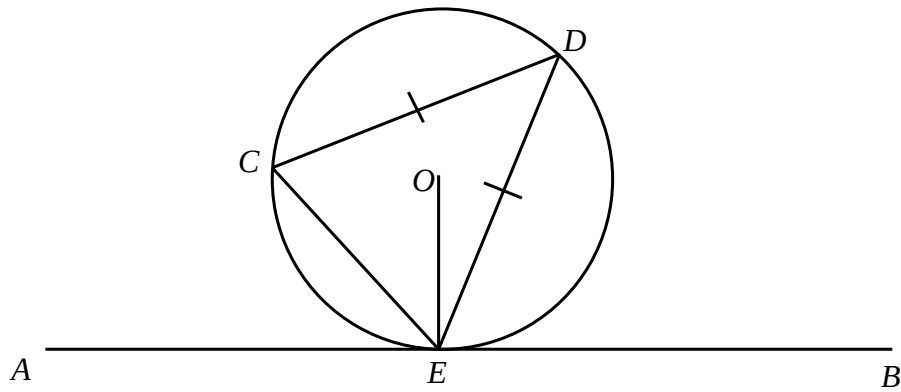
$A$ ,  $B$ ,  $C$  and  $D$  are points on the circumference of a circle, centre  $O$ .

Angle  $BOD = x^\circ$

Find the size of angle  $BCD$ , in terms of  $x$ .  
Give reasons for each stage of your working.

---

**(Total for Question 17 is 3 marks)**



$C$ ,  $D$  and  $E$  are points on a circle, centre  $O$ .  
 $AEB$  is a tangent to the circle at  $E$ .

$CD = DE$   
 Angle  $AEC = x^\circ$

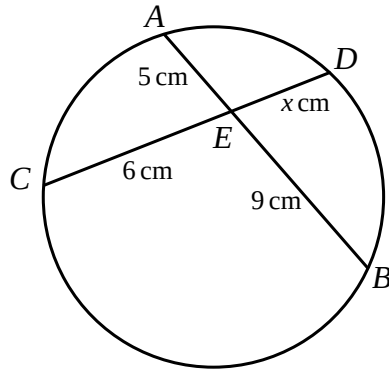
Find the size of angle  $OED$ , in terms of  $x$ .  
 Give reasons for each stage of your working.

---

(Total for Question 18 is 5 marks)



19



$AB$  and  $CD$  are chords of a circle that intersect at  $E$ .

$$AE = 5 \text{ cm}$$

$$BE = 9 \text{ cm}$$

$$CE = 6 \text{ cm}$$

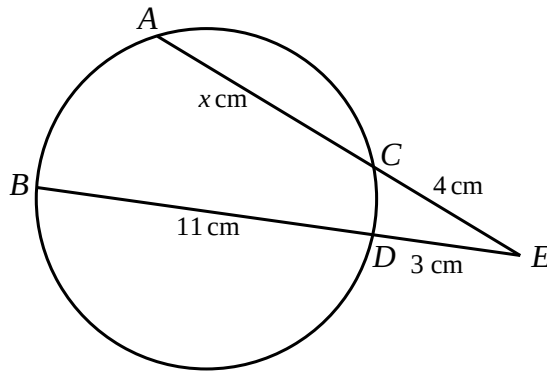
$$DE = x \text{ cm}$$

Find the value of  $x$ .

$$x = \dots\dots\dots$$

(Total for Question 19 is 2 marks)

20



$A$ ,  $B$ ,  $C$  and  $D$  are points on a circle.

$ACE$  and  $BDE$  are straight lines.

$$AC = x \text{ cm}, BD = 10 \text{ cm}, CE = 4 \text{ cm and } DE = 3 \text{ cm}$$

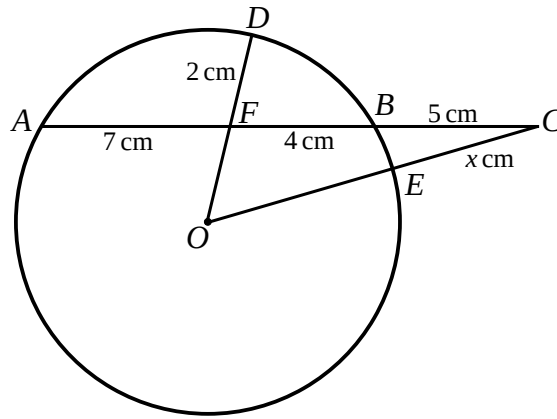
Find the value of  $x$ .

$$x = \dots\dots\dots$$

(Total for Question 20 is 3 marks)

June 2018 Paper 2H Question 22

21



$A$ ,  $D$ ,  $B$  and  $E$  are points on a circle, centre  $O$ .  
 $AFBC$ ,  $OEC$  and  $OFD$  are straight lines.

$AF = 7$  cm,  $FB = 4$  cm,  $BC = 5$  cm,  $FD = 2$  cm and  $CE = x$  cm.

Work out the value of  $x$ .  
Show your working clearly.

$x =$  .....

(Total for Question 21 is 5 marks)