## C1 Coordinate Geometry

1 The straight line $l$ has gradient -3 and passes through the point with coordinates $(3,-5)$.
a Find an equation of the line $l$.
The straight line $m$ passes through the points with coordinates $(-1,-2)$ and $(4,1)$.
b Find the equation of $m$ in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
The lines $l$ and $m$ intersect at the point $P$.
c Find the coordinates of $P$.

2 Given that the straight line passing through the points $A(2,-3)$ and $B(7, k)$ has gradient $\frac{3}{2}$,
a find the value of $k$,
b show that the perpendicular bisector of $A B$ has the equation $8 x+12 y-45=0$.
3 The vertices of a triangle are the points $A(5,4), B(-5,8)$ and $C(1,11)$.
a Find the equation of the straight line passing through $A$ and $B$, giving your answer in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
b Find the coordinates of the point $M$, the mid-point of $A C$.
c Show that $O M$ is perpendicular to $A B$, where $O$ is the origin.
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The line $l$ with equation $3 x+y-9=0$ intersects the line $m$ with equation $2 x+3 y-12=0$ at the point $A$ as shown in the diagram above.
a Find, as exact fractions, the coordinates of the point $A$.
The region $R_{1}$ is bounded by $l, m$ and the $y$-axis.
The region $R_{2}$ is bounded by $l, m$ and the $x$-axis.
b Show that the ratio of the area of $R_{1}$ to the area of $R_{2}$ is $25: 18$
5 The straight line $l$ has the equation $2 x+5 y+10=0$.
The straight line $m$ has the equation $6 x-5 y-30=0$.
a Sketch the lines $l$ and $m$ on the same set of axes showing the coordinates of any points at which each line crosses the coordinate axes.
The points where line $m$ crosses the coordinate axes are denoted by $A$ and $B$.
b Show that $l$ passes through the mid-point of $A B$.
$6 \quad$ The straight line $l$ passes through the points with coordinates $(-10,-4)$ and $(5,4)$.
a Find the equation of $l$ in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
The line $l$ crosses the coordinate axes at the points $P$ and $Q$.
b Find, as an exact fraction, the area of triangle $O P Q$, where $O$ is the origin.
c Show that the length of $P Q$ is $2 \frac{5}{6}$.
7 The point $A$ has coordinates $(-8,1)$ and the point $B$ has coordinates $(-4,-5)$.
a Find the equation of the straight line passing through $A$ and $B$, giving your answer in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
b Show that the distance of the mid-point of $A B$ from the origin is $k \sqrt{10}$ where $k$ is an integer to be found.

8 The straight line $l_{1}$ has gradient $\frac{1}{3}$ and passes through the point with coordinates $(-3,4)$.
a Find the equation of $l_{1}$ in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
The straight line $l_{2}$ has the equation $5 x+p y-2=0$ and intersects $l_{1}$ at the point with coordinates $(q, 7)$.
b Find the values of the constants $p$ and $q$.

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The diagram shows trapezium $A B C D$ in which sides $A B$ and $D C$ are parallel. The point $A$ has coordinates $(-4,2)$ and the point $B$ has coordinates $(6,6)$.
a Find the equation of the straight line passing through $A$ and $B$, giving your answer in the form $a x+b y+c=0$, where $a, b$ and $c$ are integers.
Given that the gradient of $B C$ is -1 ,
b find an equation of the straight line passing through $B$ and $C$.
Given also that the point $D$ has coordinates $(-2,7)$,
c find the coordinates of the point $C$,
d show that $\angle A C B=90^{\circ}$.
10 The straight line $l$ passes through the points $A(1,2 \sqrt{3})$ and $B(\sqrt{3}, 6)$.
a Find the gradient of $l$ in its simplest form.
b Show that $l$ also passes through the origin.
c Show that the straight line which passes through $A$ and is perpendicular to $l$ has equation

$$
x+2 \sqrt{3} y-13=0 .
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