## C4

1 Given that $y=x^{2}+3 x+5$,
and that $\quad x=(t-4)^{3}$,
a find expressions for
i $\quad \frac{\mathrm{d} y}{\mathrm{~d} x}$ in terms of $x, \quad$ ii $\frac{\mathrm{d} x}{\mathrm{~d} t}$ in terms of $t$,
b find the value of $\frac{\mathrm{d} y}{\mathrm{~d} t}$ when
i $t=5$,
ii $x=8$.

2 The variables $x$ and $y$ are related by the equation $y=x \sqrt{2 x-3}$.
Given that $x$ is increasing at the rate of 0.3 units per second when $x=6$, find the rate at which $y$ is increasing at this instant.

3 The radius of a circle is increasing at a constant rate of $0.2 \mathrm{~cm} \mathrm{~s}^{-1}$.
a Show that the perimeter of the circle is increasing at the rate of $0.4 \pi \mathrm{~cm} \mathrm{~s}^{-1}$.
b Find the rate at which the area of the circle is increasing when the radius is 10 cm .
c Find the radius of the circle when its area is increasing at the rate of $20 \mathrm{~cm}^{2} \mathrm{~s}^{-1}$.
4 The area of a circle is decreasing at a constant rate of $0.5 \mathrm{~cm}^{2} \mathrm{~s}^{-1}$.
a Find the rate at which the radius of the circle is decreasing when the radius is 8 cm .
b Find the rate at which the perimeter of the circle is decreasing when the radius is 8 cm .
5 The volume of a cube is increasing at a constant rate of $3.5 \mathrm{~cm}^{3} \mathrm{~s}^{-1}$. Find
a the rate at which the length of one side of the cube is increasing when the volume is $200 \mathrm{~cm}^{3}$,
b the volume of the cube when the length of one side is increasing at the rate of $2 \mathrm{~mm} \mathrm{~s}^{-1}$.
6


The diagram shows the cross-section of a right-circular paper cone being used as a filter funnel. The volume of liquid in the funnel is $V \mathrm{~cm}^{3}$ when the depth of the liquid is $h \mathrm{~cm}$.
Given that the angle between the sides of the funnel in the cross-section is $60^{\circ}$ as shown,
a show that $V=\frac{1}{9} \pi h^{3}$.
Given also that at time $t$ seconds after liquid is put in the funnel

$$
V=600 \mathrm{e}^{-0.0005 t},
$$

b show that after two minutes, the depth of liquid in the funnel is approximately 11.7 cm ,
c find the rate at which the depth of liquid is decreasing after two minutes.

