

1. The table gives information about the selling price and the mileages of 8 used cars.

Selling price (to the nearest £500)		Mileage (to the nearest 1000 miles)		d Rank	d^2
11 000	3	78 000	2	1	1
8500	6	65 000	3	3	9
9500	4	39 000	5	1	1
7000	7	34 000	6	1	1
12 500	2	23 000	7	5	25
5000	8	105 000	1	7	49
9000	5	48 000	4	1	1
14 000	1	20 000	8	7	49

- (a) Calculate Spearman's coefficient of rank correlation for this information. ¹³⁶

$$1 - \frac{6 \sum d^2}{n(n^2 - 1)}$$

$$1 - \frac{6(136)}{8(8^2 - 1)}$$

$$= -0.619 \text{ (3sf)} \quad \underline{\underline{-0.619}}$$

(4)

- (b) (i) Interpret the correlation between the selling price and the mileage of these used cars.

as mileage increases selling price decreases

- (ii) Comment on the strength of the correlation.

it is quite a strong correlation → close to -1 (perfect correlation) than to 0 (no correlation)

(2)

(Total for Question 1 is 6 marks)

2. Mrs Smith and Mrs Patel ranked the work of 8 students. The table gives information about their ranks.

Student	Rank (Mrs Smith)	Rank (Mrs Patel)	d	d^2
A	4	6	2	4
B	8	4	4	16
C	1	3	2	4
D	6	1	5	25
E	2	7	5	25
F	7	8	1	1
G	3	2	1	1
H	5	5	0	0

- (i) Calculate Spearman's coefficient of rank correlation for this information.

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$$1 - \frac{6 \sum d^2}{n(n^2 - 1)}$$

$$1 - \frac{6(76)}{8(8^2 - 1)}$$

$$= 0.095 \text{ (3 s.f.)}$$

0.095

- (ii) Interpret your answer.

There does not seem to be a relationship between the ranks of Mrs Smith & Mrs Patel

(Total for Question 2 is 4 marks)

3. The table gives information about the heights, in cm, of ten athletes and their positions in a throwing competition.

Athlete	Height (cm)	Position	Rank Height	d	d^2
A	112	8	10	2	4
B	114	9	9	0	0
C	123	7	8	1	1
D	128	5	7	2	4
E	134	10	6	4	16
F	146	3	5	2	4
G	148	4	4	0	0
H	151	6	3	3	9
I	154	1	2	1	1
J	158	2	1	1	1

- (a) Work out Spearman's rank correlation coefficient for these data.

40

You may use the blank columns in the table to help with your calculations.

$$1 - \frac{6 \sum d^2}{n(n^2 - 1)}$$

$$1 - \frac{6(40)}{10(10^2 - 1)}$$

$$= 0.758 \text{ (3sf)}$$

0.758

(3)

- (b) Interpret your answer to part (a).

As the athletes height increases their position increases. (positive correlation)

(1)

(Total for Question 3 is 4 marks)

4. Dr Farah collected some information about the Body Mass Index (BMI) and the finishing position in a marathon for each of ten male adults.

The table shows this information.

Adult	BMI	Finishing position	Rank of BMI	d	d^2
A	18.4	3	10	7	49
B	19.5	2	9	7	49
C	19.8	1	8	7	49
D	20.5	6	7	1	1
E	21.2	4	6	2	4
F	22.5	5	5	0	0
G	23.7	9	4	5	25
H	25.3	10	3	7	49
I	26.7	7	2	5	25
J	29.3	8	1	7	49

- (a) Calculate Spearman's coefficient of rank correlation for this information. 300

You may use the columns in the table to help with your calculations.

$$1 - \frac{6(300)}{10(10^2 - 1)} = \frac{-0.818(354)}{(3)}$$

- (b) (i) Describe the correlation.

Negative.

- (ii) Interpret the correlation in the context of the information in the table.

People with a higher BMI took longer to complete the race.

(2)

(Total for Question 4 is 5 marks)

5 8 people were in a cake baking competition.

Judge X and Judge Y each put the cakes in rank order.

Rank 1 is for the best cake.

Here are the results.

Cake	Judge X	Judge Y	d	d^2
A	1	5	4	16
B	6	8	2	4
C	2	4	2	4
D	5	2	3	9
E	4	1	3	9
F	3	7	4	16
G	7	6	1	1
H	8	3	5	25

- (a) Work out Spearman's coefficient of rank correlation for the information in the table. You may use the blank columns in the table to help you with your calculations.

$$1 - \frac{6 \sum d^2}{n(n^2 - 1)}$$

$$1 - \frac{6(84)}{8(8^2 - 1)} = 0$$

..... 0 (3)

- (b) Interpret your answer to part (a).

..... There is no relationship between
 the rank of Judge X and Judge Y

(1)

(Total for Question 5 is 4 marks)

